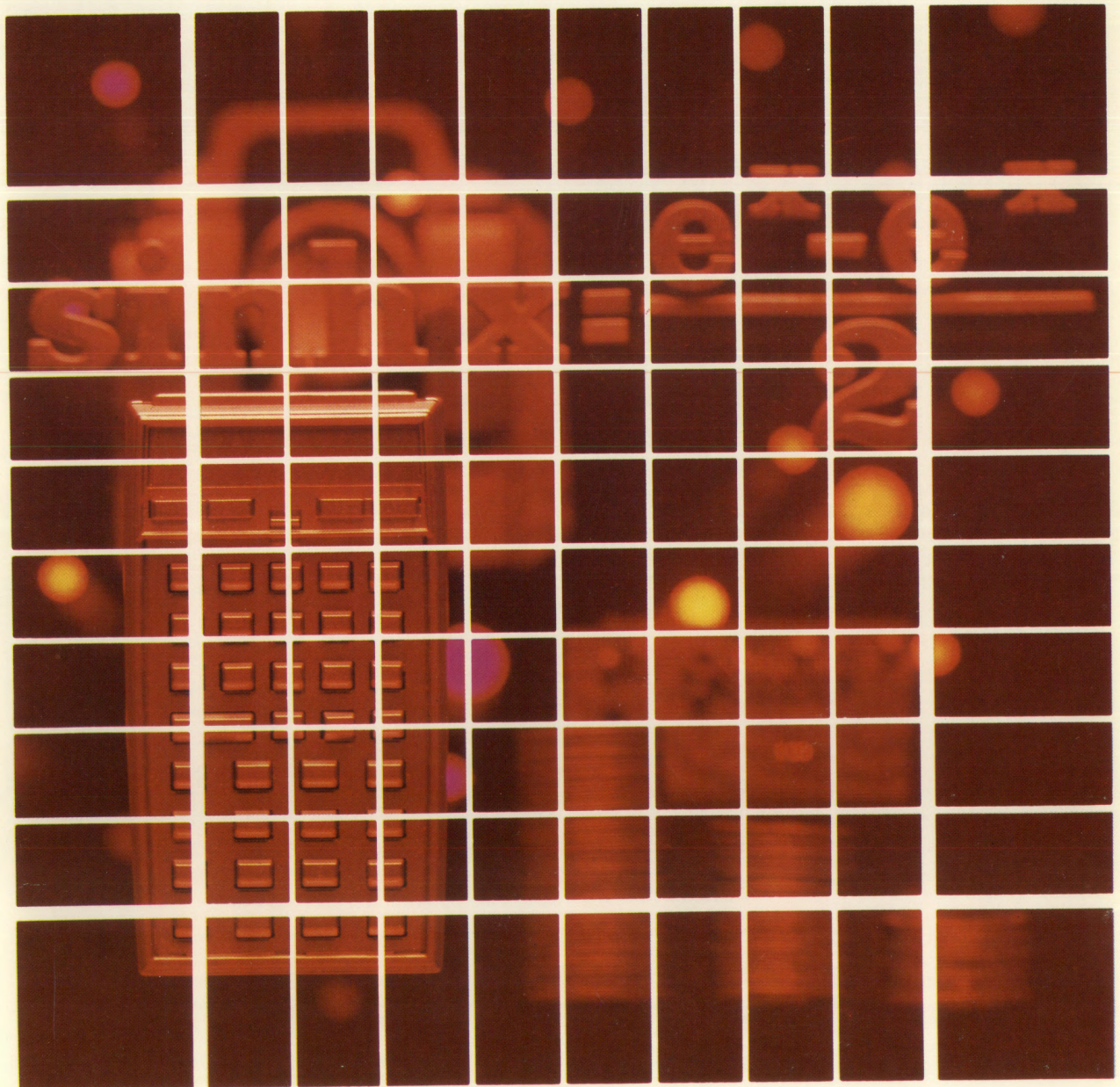


HEWLETT-PACKARD

HP-41C

USERS'  
LIBRARY SOLUTIONS  
Solar Engineering



## **NOTICE**

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## INTRODUCTION

This HP-41C Solutions book was written to help you get the most from your calculator. The programs were chosen to provide useful calculations for many of the common problems encountered.

They will provide you with immediate capabilities in your everyday calculations and you will find them useful as guides to programming techniques for writing your own customized software. The comments on each program listing describe the approach used to reach the solution and help you follow the programmer's logic as you become and expert on your HP calculator.

### KEYING A PROGRAM INTO THE HP-41C

There are several things that you should keep in mind while you are keying in programs from the program listings provided in this book. The output from the HP 82143A printer provides a convenient way of listing and an easily understood method of keying in programs without showing every keystroke. This type of output is what appears in this handbook. Once you understand the procedure for keying programs in from the printed listings, you will find this method simple and fast. Here is the procedure:

1. At the end of each program listing is a listing of status information required to properly execute that program. Included is the SIZE allocation required. Before you begin keying in the program, press **XEQ** **ALPHA** SIZE **ALPHA** and specify the allocation (three digits; e.g., 10 should be specified as 010).  
Also included in the status information is the display format and status of flags important to the program. To ensure proper execution, check to see that the display status of the HP-41C is set as specified and check to see that all applicable flags are set or clear as specified.
2. Set the HP-41C to PRGM mode (press the **PRGM** key) and press **▀** **GTO** **◊** **◊** to prepare the calculator for the new program.
3. Begin keying in the program. Following is a list of hints that will help you when you key in your programs from the program listings in this handbook.
  - a. When you see " (quote marks) around a character or group of characters in the program listing, those characters are ALPHA. To key them in, simply press **ALPHA**, key in the characters, then press **ALPHA** again. So "SAMPLE" would be keyed in as **ALPHA** "SAMPLE" **ALPHA**.
  - b. The diamond in front of each LBL instruction is only a visual aid to help you locate labels in the program listings. When you key in a program, ignore the diamond.
  - c. The printer indication of divide sign is /. When you see / in the program listing, press **+**.
  - d. The printer indication of the multiply sign is  $\times$ . When you see  $\times$  in the program listing, press **x**.
  - e. The † character in the program listing is an indication of the **APPEND** function. When you see †, press **▀** **APPEND** in ALPHA mode (press **▀** and the K key).
  - f. All operations requiring register addresses accept those addresses in these forms:

nn (a two-digit number)

IND nn (INDIRECT: **▀**, followed by a two-digit number)

X, Y, Z, T, or L (a STACK address: **◊** followed by X, Y, Z, T, or L)

IND X, Y, Z, T or L (INDIRECT stack: **▀** **◊** followed by X, Y, Z, T, or L)

Indirect addresses are specified by pressing **▀** and then the indirect address. Stack addresses are specified by pressing **◊** followed by X, Y, Z, T, or L. Indirect stack addresses are specified by pressing **▀** **◊** and X, Y, Z, T, or L.

#### Printer Listing

```

01 †LBL "SAM
PLE"
02 "THIS IS
A"
03 †SAMPLE
"
04 AVIEW
05 6
06 ENTER†
07 -2
08 /
09 ABS
10 STO IND
L
11 "R3="
12 ARCL 03
13 AVIEW
14 RTN
  
```

#### Keystrokes

```

▀ LBL ALPHA SAMPLE ALPHA
ALPHA THIS IS A ALPHA
ALPHA ▀ APPEND SAMPLE
▀ AVIEW ALPHA
6
ENTER+
2 CHS
+
XEQ ALPHA ABS ALPHA
STO ◊ L
ALPHA R3= ▀ ARCL 03
▀ AVIEW
ALPHA
▀ RTN
  
```

#### Display

```

01 LBLT SAMPLE
02T THIS IS A
03T † SAMPLE
04 AVIEW
05 6
06 ENTER↑
07 -2
08 /
09 ABS
10 STO IND L
11T R3=
12 ARCL 03
13 AVIEW
14 RTN
  
```

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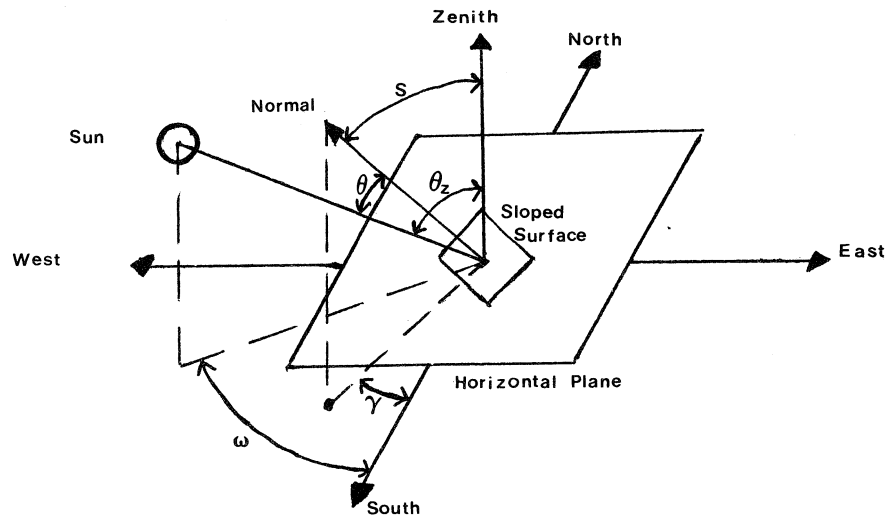
*1.	SOLAR-BEAM IRRADIATION.....	1
	This program estimates radiation impingement on a surface of any orientation and location on the earth. Sunrise and sunset times are also available.	
2.	SUN ALTITUDE, AZIMUTH, SOLAR POND ABSORPTION.....	11
	This program computes the exact position of the sun at any time of day on any date as well as the percent of radiation that will enter a solar pond of a given index of refraction.	
3.	ENERGY EQUIVALENTS-FUELS AND PRICES.....	17
	This program converts amounts and prices between 8 different fuel and energy units. Efficiencies may be included.	
*4.	HEAT EXCHANGERS.....	22
	Correlates heat transfer for counterflow, parallel flow, parallel-counterflow and crossflow heat exchangers.	
5.	VIEW FACTOR.....	38
	Calculates the amount of energy leaving one surface that gets to another surface.	
6.	HEAT TRANSFER THROUGH COMPOSITE CYLINDERS AND WALLS.....	44
	Calculates the heat transfer coefficient.	
7.	BLACK BODY THERMAL RADIATION.....	49
	Calculates thermal radiation as a function of temperature and wavelength for black bodies.	
8.	ECONOMIC BREAK EVEN FOR SOLAR EQUIPMENT.....	56
	Calculates the number of years necessary for solar equipment to pay for itself.	
9.	SOLAR PANEL ARRAY.....	61
	This program calculates the distance between tilted solar panels so that no shading will occur.	
10.	CONDUIT FLOW.....	68
	Solves a variety of problems involving viscous conduit flow.	
*	Requires an additional memory module.	



## SOLAR-BEAM IRRADIATION

(Requires an additional memory module.)

This program enables the user to estimate solar-beam radiation impingement on a surface of any orientation and location on the earth for any day of the year. No prior knowledge of solar orbital mechanics is necessary. Solar-beam radiation rates may be estimated for any hour of the day. The program allows the user to integrate the total beam radiation over a given span of time during the day. Sunrise and sunset times may be calculated for any day of the year at any location on the earth.



Angle of incidence ( $\theta$ ) of beam radiation.

$$\begin{aligned} \cos \theta = & \sin \delta \sin \phi \cos \delta - \sin \delta \cos \phi \sin S \cos \gamma \\ & + \cos \delta \cos \phi \cos S \cos \omega + \cos \delta \sin \phi \sin S \cos \gamma \cos \omega \\ & + \cos \delta \sin S \sin \gamma \sin \omega \end{aligned}$$

WHERE:  $\delta$  = Declination (i.e., angular position of sun at solar noon with respect to plane of equator; north is positive (see below))

$\phi$  = Latitude; North is positive

$\omega$  = Surface azimuth angle, the deviation of the normal to the surface from local meridian. The zero point is due south, east is positive and west is negative.

$\theta$  = Angle of incidence of beam radiation, measured between beam and normal to the plane.

Declination ( $\delta$ ) (Approximate)

$$\delta = 23.45 \sin [.9863 (284 + \eta)]$$

Where:  $\eta$  = Numbered day of year (i.e., February 15 is 46th day of year.)

Calculation of solar angle ( $\omega$ )

$$\text{Solar time} = \text{Standard Time} + E + 4 (L_{st} - L_{loc})$$

Where: E = Equation of Time

$$E = 8 \text{ SIN } (1.06 \eta - 48) + 10 \text{ SIN } [1.9 (1.1 \eta - 30)]$$

$L_{st}$  = Standard Meridian for local time zone

(Standard meridians for Continental U.S. time zones are:

Atlantic, 60° W; Eastern, 75° W; Central, 90° W;

Mountain, 105° W; and Pacific, 120° W.)

$L_{loc}$  = Longitude of location in question

$$\omega = (12 - \text{solar time}) \times 15$$

Where:  $\omega$  = hour angle in degrees (positive for morning and negative for afternoon.)

Zenith Angle  $\theta_z$

$$\text{COS } \theta_z = \text{SIN } \delta \text{ SIN } \phi + \text{COS } \delta \text{ COS } \phi \text{ COS } \omega$$

Radiant Energy (G) received at surface

$$G = G_0 \times t^m \text{ COS } \theta$$

Where:  $G_0$  = Solar constant 442.4 BTU HR °F FT<sup>2</sup>

t = Transmission coefficient for unit air mass

(cloudy, 0.62; mean value, 0.70; clear day, 0.81)

m = Secant of zenith angle; SEC  $\theta_z$

Time of sunrise and sunset

$$\text{COS } \omega_s = -\text{TAN } \phi \text{ TAN } \delta$$

WHERE:  $\omega_s$  = Sunrise hour angle

$$\text{Sunrise solar time} = 12 - \frac{\omega_s}{15}$$

$$\text{Sunrise standard time} = \text{Sunrise solar time} - E - 4 (L_{st} - L_{loc})$$

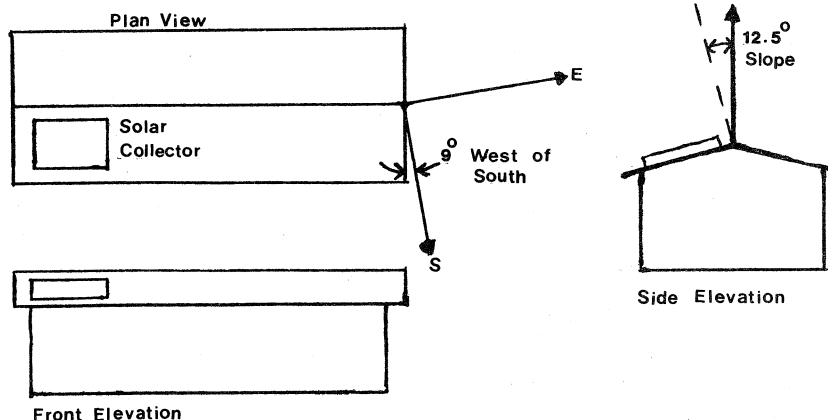
$$\text{Sunset solar time} = 12 + \frac{\omega_s}{15}$$

$$\text{Sunset standard time} = \text{Sunset solar time} - E - 4 (L_{st} - L_{loc})$$

The total irradiation during a time period

$$G_0 \int_{\omega_2}^{\omega_1} t \text{ SEC } \theta_z \text{ COS } \theta \, d\omega = \Sigma G(\omega_1 - \omega_2)$$

## EXAMPLE:



Find solar-beam radiation rate impinging on a solar collector at 10:45 a.m. and 2:20 p.m., and the total energy from 10:30 a.m. to 3:20 p.m. Also, what is the time of sunrise and sunset? The solar collector is mounted on a roof sloped  $12.5^\circ$  from horizontal and pointed  $9^\circ$  west of south. The date is September 2, 1981 and is an average clear day in Los Angeles, California. The approximate coordinates are  $34^\circ 10'$  north latitude and  $118^\circ 21'$  west longitude. The standard time meridian for Pacific Standard Time is  $120^\circ$  W.

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 026

[XEQ] [ALPHA] IRRAD [ALPHA]

9.021981 [R/S]

34.1 [R/S]

118.21 [R/S]

120 [R/S]

12.5 [R/S]

9 [CHS] [R/S]

.7 [R/S]

10.45 [A]

14.20 [A]

10.30 [ENTER $\uparrow$ ]15.20 [ENTER $\uparrow$ ]

.5 [B]

If a collector of  $150 \text{ ft}^2$  is used, how many BTU is this.

150 [X]

[C]

[R/S]

MM.DDYYY ?

LAT. ?

LONG.?

TIME MER. ?

SLOPE ?

AZIMUTH ?

TRAN. COEF. ?

A, B OR C ?

 $G = 267 \text{ (BTU/HR FT}^2\text{)}$  $G = 220 \text{ (BTU/HR FT}^2\text{)}$  $\Sigma G = 1,122 \text{ (BTU/FT}^2\text{)}$ 

181840 (BTU)

SUN R = 5:34 (AM)

SUN S = 18:14 (6:14 PM)

# User Instructions

				SIZE: 026
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Load the program.			
2	Initialize.		[XEQ] IRRAD	MM.DDYYYY ?
3	Key in the date.	date	[R/S]	LAT
4	Key in the latitude (neg. for south)			
	in degrees, minutes and seconds.	$\phi$	[R/S]	LONG. ?
5.	Key in the longitude (neg. for east)			
	in degrees, minutes and seconds.	$L_{loc}$	[R/S]	TIME MER. ?
6	Key in the time meridian for			
	local standard time:			
	Atlantic = 60° W			
	Eastern = 75° W			
	Central = 90° W			
	Mountain = 105° W			
	Pacific = 120° W	$L_{st}$	[R/S]	SLOPE ?
7	Key in the slope of the plane in decimal			
	degrees.	S	[R/S]	AZIMUTH ?
8	Key in the surface azimuth in degrees,			
	minutes, seconds:			
	East is positive			
	South is zero			
	West is negative	$\gamma$	[R/S]	TRAN. COEF.?
9	Key the solar transmission coefficient:			
	Cloudy = .62			
	Mean = .70			
	Clear = .81	t	[R/S]	A, B OR C?





# Program Listings

01 *LBL "IRR AD"		50 HR	
02 SF 21	Input	51 STO 00	
03 FIX 0		52 1	
04 CF 29		53 P-R	
05 SF 27		54 STO 11	
06 "MM.DDYY YY ?"		55 RDN	
07 CF 22		56 STO 10	
08 RCL 06		57 "LONG. ? "	
09 PROMPT	Date	58 RCL 02	Longitude
10 FC?C 22		59 PROMPT	
11 GTO 00		60 FS?C 22	
12 INT	Calculate	61 HR	
13 STO 01	DDY	62 STO 02	
14 LASTX		63 "TIME ME R. ?"	
15 FRC		64 RCL 01	
16 100		65 PROMPT	Time Meridian
17 *		66 STO 01	
18 INT		67 "SLOPE ? "	
19 STO 06		68 RCL 03	
20 LASTX		69 PROMPT	Slope
21 FRC		70 STO 03	
22 2500		71 1	
23 *		72 P-R	
24 FRC		73 STO 13	
25 STO 02		74 RDN	
26 RCL 01		75 STO 12	
27 30.56		76 "AZIMUTH ?"	
28 *		77 RCL 04	
29 INT		78 CF 22	
30 30		79 PROMPT	Azimuth
31 -		80 FS?C 22	
32 ST+ 06		81 HR	
33 RCL 02		82 STO 04	
34 ENTER↑		83 1	
35 X≠0?		84 P-R	
36 /		85 STO 15	
37 1		86 RDN	
38 +		87 STO 14	
39 2		88 "TRAN. C DEF. ?"	
40 RCL 01		89 RCL 07	
41 X<=Y?		90 PROMPT	Transmission coefficient
42 GTO 00		91 STO 07	
43 RCL Z		92 RCL 06	
44 ST- 06		93 284	
45 *LBL 00		94 +	Set up
46 "LAT. ?"		95 .986	
47 RCL 00	Latitude		
48 PROMPT			
49 FS?C 22			

# Program Listings

96 *		146 RCL 19	
97 SIN		147 *	
98 23.45		148 +	
99 *		149 1/X	
100 STO 05	δ	150 6	
101 1		151 X<=Y?	
102 P-R		152 GTO 03	
103 STO 17		153 RDN	
104 RDN		154 RCL 07	
105 STO 16		155 X<>Y	
106 RCL 06		156 Y↑X	
107 81		157 442.4	Solar Constant
108 -		158 *	
109 .989		159 RCL 22	
110 *		160 *	
111 ENTER↑		161 X>0?	
112 SIN		162 GTO 04	
113 1.5		163*LBL 03	
114 *		164 0	
115 CHS		165*LBL 04	Output of G
116 X<>Y		166 "G="	
117 ENTER↑		167 ARCL X	
118 COS		168 AVIEW	
119 7.53		169 RTN	
120 *		170*LBL B	
121 CHS		171 15	
122 X<>Y		172 *	
123 2		173 STO 25	
124 *		174 RDN	
125 SIN		175 HR	
126 9.87		176 X<>Y	
127 *		177 HR	
128 +		178 X<>Y	
129 +		179 CF 00	
130 CHS		180 XEQ 20	
131 60		181 STO 19	
132 /		182*LBL 01	
133 RCL 01		183 RCL 23	
134 RCL 02		184 RCL 24	
135 -		185 -	
136 15		186 RCL 25	
137 /		187 X<=Y?	
138 +		188 GTO 02	
139 STO 09		189 RDN	
140 "A, B OR		190 STO 25	
C?"	Set up done	191 SF 01	
141 PROMPT	-----	192*LBL 02	
142*LBL A		193 RCL 23	
143 HR	Time	194 RCL 25	
144 SF 00		195 2	
145 XEQ 20		196 /	

$$\int_{T_1}^{T_2} G$$

# Program Listings

197 -		248 X<>Y	
198 ENTER↑		249 -	
199 COS		250 15	
200 RCL 21		251 *	
201 *		252 STO 24	
202 X<>Y		253 FS? 00	
203 1/X		254 GTO 00	
204 RCL 22		255 RDN	
205 *		256 RCL 09	
206 +		257 +	
207 RCL 20		258 12	
208 +		259 X<>Y	
209 RCL 23		260 -	
210 RCL 25		261 15	
211 2		262 *	
212 /		263 STO 23	
213 -		264 0	
214 COS		265 STO 08	
215 RCL 19		266 GTO 02	
216 *		267*LBL 00	
217 RCL 18		268 1	
218 +		269 P-R	
219 1/X		270 STO 19	
220 RCL 07		271 RDN	
221 X<>Y		272 STO 18	
222 Y↑X		273*LBL 02	
223 *		274 RCL 16	
224 RCL 25		275 RCL 10	
225 *		276 *	
226 15		277 RCL 13	
227 /		278 *	
228 X<0?		279 RCL 16	
229 0		280 RCL 11	
230 ST+ 08		281 *	
231 RCL 23		282 RCL 12	
232 RCL 25		283 *	
233 -		284 RCL 15	
234 STO 23		285 *	
235 FC?C 01		286 -	
236 GTO 01		287 STO 20	
237 RCL 08		288 RCL 17	
238 442.4	Solar Constant	289 RCL 11	
239 *	Output ΣG	290 *	
240 "ΣG="		291 RCL 13	
241 ARCL X		292 *	
242 AVIEW		293 FC? 00	
243 RTN		294 GTO 00	
244*LBL 20	Common	295 RCL 19	
245 RCL 09	Subroutine	296 *	
246 +		297 +	
247 12		298*LBL 00	







## SUN ALTITUDE, AZIMUTH, SOLAR POND ABSORPTION

This program computes the Sun's azimuth and altitude ( $Z_n$  and  $H_c$ ) in decimal degrees given any latitude, longitude, date and time. Then, if you wish, you can input an index of refraction for any fluid and calculate the percent of radiation which would penetrate the surface of the fluid.

The almanac equations used in this program have been checked to the end of the century for accuracy and found to be accurate to within a .2' arc.

### Example:

Find the Sun's azimuth, altitude, and the fraction of the Sun's radiation which will penetrate the surface of a solar pond under the following circumstances:

Date	9/1/79
Latitude	44°34'
Longitude	123°17'
GMT	20:00:00 (Noon PST)
Index of refraction	1.33

### Keystrokes:

```
[XEQ] [ALPHA] SIZE [ALPHA] 009
[XEQ] [ALPHA] ALMANAC [ALPHA]
9.011979 [R/S]
44.34 [R/S]
123.17 [R/S]
20 [R/S]
[R/S]
[B]
1.33 [R/S]
```

### Display:

```
MM.DDYYYY ?
LAT ?
LONG ?
GMT ?
ZN=174.5022
HC=53.5985
N ?
%E=97.7355
```

Find the same information for 5 hours later.

Keystrokes:

[A]

[R/S]

[R/S]

[R/S]

25 [R/S]

[R/S]

[B]

[R/S]

Display:

MM.DDYyyy ?

LAT ?

LONG ?

GMT ?

ZN=262.9527

HC=18.7391

N ?

%E=85.1269





# Program Listings

01 *LBL "ALM ANAC"	Initialize	50 20	
02 SF 27	-----	51 *	
03 *LBL A		52 STO 04	
04 SF 21		53 SIN	
05 CF 22		54 4	
06 "MM.DDYY YY ?"		55 *	
07 PROMPT	Input date	56 50941	
08 FC?C 22	-----	57 +	
09 GTO 00		58 RCL 06	
10 INT		59 7	
11 STO 06	Calculate DOY and	60 *	
12 LASTX	longitude of	61 +	
13 FRC	Moon's ascending	62 896	
14 100	node	63 /	
15 *		64 -	
16 INT		65 ST- 03	
17 STO 03		66 360	
18 LASTX		67 ST* 03	
19 FRC		68 *LBL 00	
20 1 E4		69 "LAT ?"	----- Input other quantities
21 *		70 PROMPT	
22 X<> Z		71 HR	
23 3056		72 FS?C 22	
24 %		73 STO 01	
25 INT		74 "LONG ?"	
26 ST+ 03		75 PROMPT	
27 R↑		76 HR	
28 STO 04		77 FS?C 22	
29 RCL 06		78 STO 00	
30 3		79 "GMT ?"	
31 X>Y?		80 PROMPT	
32 1		81 HR	
33 RCL 04		82 15	
34 4		83 *	
35 /		84 FS?C 22	
36 FRC		85 STO 02	
37 +		86 RCL 02	
38 1		87 STO 05	
39 X<>Y		88 RCL 03	
40 X=Y?		89 +	
41 2		90 365.25	
42 RCL 04		91 /	
43 7		92 118.1	
44 -		93 RCL 04	
45 RCL 03		94 968	
46 365.25		95 /	
47 /		96 -	
48 +		97 +	
49 STO 06		98 .2	
		99 P-R	
		100 9.58	
			----- Calculate $Z_n$ and $H_c$

# Program Listings

101 -	Semidiameter	152 "ZN="	Input n
102 *		153 ARCL X	
103 +		154 AVIEW	
104 RCL 04		155 "HC="	
105 427		156 ARCL 06	
106 /		157 AVIEW	
107 RCL 04		158 RTN	
108 COS		159 LBL B	
109 -		160 "N ?"	
110 8531.5		161 PROMPT	
111 -		162 FS?C 22	
112 360		163 STO 08	
113 /		164 90	
114 CHS	165 RCL 06		
115 X<>Y	166 -		
116 -1	167 STO 05		
117 P-R	168 SIN		
118 RDN	169 RCL 08		
119 P-R	170 /		
120 R↑	171 ASIN		
121 R-P	172 COS		
122 RDN	173 STO 07		
123 X<>Y	174 RCL 08		
124 STO 07	175 *		
125 ASIN	176 RCL 05		
126 STO 06	177 COS		
127 RDN	178 +		
128 -	179 1/X		
129 ST+ 05	180 X↑2		
130 RCL 05	181 RCL 05		
131 RCL 00	182 COS		
132 -	183 RCL 08		
133 RCL 06	184 *		
134 COS	185 RCL 07		
135 P-R	186 +		
136 RCL 01	187 1/X		
137 STO 06	188 X↑2		
138 X<>Y	189 +		
139 P-R	190 2		
140 X<> 06	191 *		
141 RCL 07	192 RCL 08		
142 P-R	193 *		
143 X<> 06	194 RCL 07		
144 +	195 *		
145 ASIN	196 RCL 05		
146 X<> 06	197 COS		
147 -	198 *		
148 R-P	199 100		
149 RDN	200 *		
150 180	201 "%E="		
151 +	202 ARCL X		
	203 AVIEW		
	204 RTN		
	205 .END.		





## ENERGY EQUIVALENTS - FUELS AND PRICES

Given an amount of fuel or energy expressed in one of the units in Table I, this program converts to an equivalent amount of another of the fuels or energy units in Table I. Also, given the price per unit of two fuels or energy units the program will convert an amount spent on one into an amount spent on the other. You may also include efficiencies between conversions. For example coal to electricity is not 100% efficient.

TABLE I

1 Barrel of Oil	= 1 BBL = 5.8 MBTU
1000 Cubic Feet of Gas	= 1 TCF = 1.03 MBTU
1 Gigajoule	= 1 GJ = 1.055 MBTU
1 Short Ton of Eastern Bituminous Coal	= 1 STE = 26 MBTU
1 Short Ton of Western Coal	= 1 STW = 18 MBTU
1 Megawatt-hour	= 1 MWH = 3.412 MBTU
1 Pound $U_{308}$	= 1 U308 = 220 MBTU*
1 Million British Thermal Units	= 1 MBTU

\* All  $U^{235}$  atoms fissioned

Example:

How many Gigajoules can you get from 20,000 cubic feet of gas if the overall efficiency is 30%.

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 005

UNITS 1 ?

[XEQ] [ALPHA] ENERGY [ALPHA]

\$ ?

TCF [R/S]

UNITS 2 ?

[R/S]

\$ ?

GJ [R/S]

% FOR 1 TO 2

[R/S]

READY

30 [R/S]

5.86 GJ

20 [B]

If you wanted 10 GJ how many thousand cubic feet of gas are required?

10 [C]

31.14 TCF

# User Instructions

				SIZE: 005
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Load the program.			
2	Initialize.		[XEQ]ENERGY	UNITS 1 ?
3	Key in the units for units 1.	Units*	[R/S]	\$ ?
4	Key in the price per unit of unit 1.			
	Just press [R/S] if not needed.	\$	[R/S]	UNITS 2 ?
5	Key in the units for units 2.	Units*	[R/S]	\$ ?
6	Key in the price per unit of unit 2. Just			
	press [R/S] if not needed.	\$	[R/S]	% FOR 1 TO 2
7	Key in the conversion efficiency to con-			
	vert from unit 1 to unit 2 if different			
	from %100, otherwise just press [R/S].	%	[R/S]	READY
8	To convert an amount from 1 to 2			
9	Key in amount of 1.	A <sub>1</sub>	[B]	( ) (UNITS 2)
10	To convert an amount from 2 to 1			
11	Key in amount of 2.	A <sub>2</sub>	[C]	( ) (UNITS 1)
12	To convert price 1 to 2			
13	Key in price 1.	P <sub>1</sub>	[D]	\$( ) (UNITS 2)
14	To convert price 2 to 1			
15	Key in price 2.	P <sub>2</sub>	[E]	\$( ) (UNITS 1)
16	Repeat steps 8-15 as desired.			
17	To change any or all of steps 3-6 press [A]			
	and go to step 3. For inputs that do not			
	change just press [R/S].		[A]	UNITS 1 ?
	*Key in an abbreviation from Table I.			

# Program Listings

01*LBL "ENE RGY"	Initialize	48 ARCL X	
02 SF 27		49 "F "	
03 1		50 ARCL 01	
04 STO 02		51 PROMPT	
05*LBL A		52*LBL D	-----
06 AON	Input	53 RCL 03	\$
07 CF 23		54 /	Forward
08 "UNITS 1 ?"		55 XEQ 01	
09 PROMPT		56 RCL 04	
10 FS?C 23		57 *	
11 ASTO 01		58 "\$"	
12 RCL 03		59 GTO 03	-----
13 "\$ ?"		60*LBL E	\$
14 AOFF		61 RCL 04	Backward
15 PROMPT		62 /	
16 STO 03		63 XEQ 02	
17 "UNITS 2 ?"		64 RCL 03	
18 AON		65 *	
19 PROMPT		66 "\$"	
20 FS?C 23		67 GTO 04	-----
21 ASTO 00		68*LBL 01	
22 AOFF		69 CF 00	
23 "\$ ?"		70 XEQ IND	
24 RCL 04		01	Conversion
25 PROMPT		71 SF 00	
26 STO 04		72 XEQ IND	
27 "% FOR 1 TO 2"		00	
28 CF 22		73 RCL 02	
29 PROMPT		74 *	
30 100		75 RTN	
31 /		76*LBL 02	
32 FS?C 22		77 CF 00	
33 STO 02		78 XEQ IND	
34 "READY"		00	
35 PROMPT		79 SF 00	
36*LBL B		80 XEQ IND	
37 XEQ 01	Forward	01	
38 CLA		81 RCL 02	
39*LBL 03		82 /	
40 ARCL X		83 RTN	
41 "F "		84*LBL "BBL	-----
42 ARCL 00		..	Conversion
43 PROMPT		85 5.8	constants
44*LBL C		86 GTO 05	
45 XEQ 02		87*LBL "TCF	
46 CLA		..	
47*LBL 04		88 1.03	
	Backward	89 GTO 05	
		90*LBL "GJ"	
		91 1.055	
		92 GTO 05	

# Program Listings

93*LBL "STE		51	
..			
94 26			
95 GTO 05			
96*LBL "STW			
..			
97 18			
98 GTO 05			
99*LBL "MWH			
..			
100 3.412		60	
101 GTO 05			
102*LBL "U30			
8"			
103 220			
104 GTO 05			
105*LBL "MBT			
U"			
106 1			
107*LBL 05			
108 FS? 00		70	
109 1/X			
110 *			
111 RTN			
112 .END.			
30		80	
40		90	
50		00	



## HEAT EXCHANGERS

(Requires one memory module)

This program allows analysis of counterflow, parallel flow, parallel-counterflow, and crossflow heat exchangers.

Figure 1:

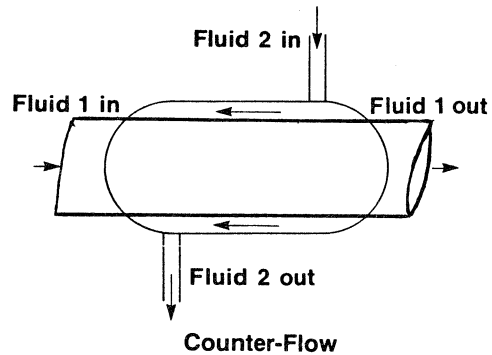


Figure 2:

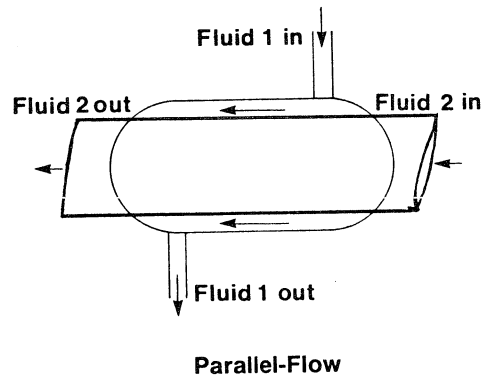


Figure 3:

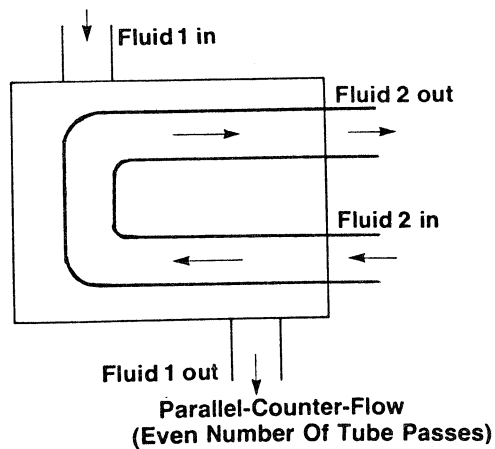
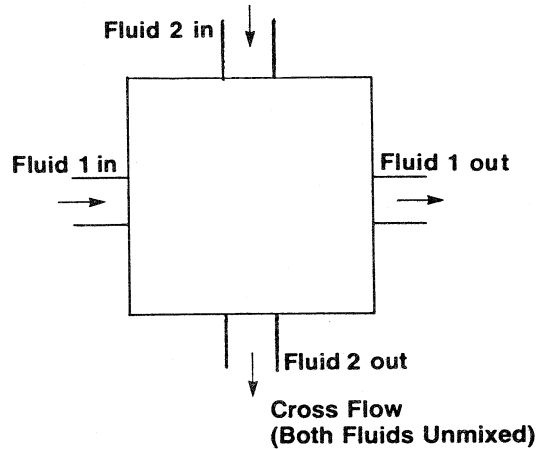


Figure 4:



Equations:

Heat exchanger effectiveness  $E$  is the ratio of actual heat transfer to maximum possible heat transfer.

$$E = \frac{Q}{C_{\min} (T_{hin} - T_{cin})} = \frac{C_h (T_{hin} - T_{ho})}{C_{\min} (T_{hin} - T_{cin})} = \frac{C_c (T_{co} - T_{cin})}{C_{\min} (T_{hin} - T_{cin})}$$

where:

$Q$  is the actual heat transfer.

$T_{hin}$  and  $T_{cin}$  are the inlet temperatures of the hot and cold fluids respectively.

$T_{ho}$  and  $T_{co}$  are the outlet temperatures of the hot and cold fluids respectively.

$C_h$  and  $C_c$  are the heat capacities of the hot and cold fluids, respectively, e.g.,  $C_h = m_h \times c_{ph}$ , where  $m_h$  is the flow rate and  $c_{ph}$  is the specific heat capacity of the hot fluid.

$C_{\min}$  and  $C_{\max}$  (which are used later) are the smaller and larger values of  $C_h$  and  $C_c$ .

Effectiveness can be related to the product of the surface area of the heat exchanger and the overall heat transfer coefficient for specific geometries. This product is designated AU. The geometries considered in this pac have the following correlations:

Counterflow (see figure 1)

$$E = \frac{1 - e^{-\frac{AU}{C_{\min}} \left(1 - \frac{C_{\min}}{C_{\max}}\right)}}{1 - \left(\frac{C_{\min}}{C_{\max}}\right) e^{-\frac{AU}{C_{\min}} \left(1 - \frac{C_{\min}}{C_{\max}}\right)}}$$

For  $C_{\min}/C_{\max} = 1$

$$E = \frac{AU/C_{\min}}{1 + AU/C_{\min}}$$

Parallel Flow (see figure 2)

$$E = \frac{1 - e^{-\frac{AU}{C_{\min}} (1 + C_{\min}/C_{\max})}}{1 + C_{\min}/C_{\max}}$$

For  $C_{\min}/C_{\max} = 0$ ,  $C_{\min}$  is set to 1.

Parallel-Counterflow (well mixed with an even number of tube passes; see Figure 3)

$$E = \frac{2}{\left(1 + \frac{C_{\min}}{C_{\max}}\right) + \sqrt{1 + \left(\frac{C_{\min}}{C_{\max}}\right)^2} \left[\frac{1 + e^{-x}}{1 - e^{-x}}\right]}$$

where:

$$x = \frac{AU}{C_{\min}} \sqrt{1 + \left(\frac{C_{\min}}{C_{\max}}\right)^2}$$



Crossflow (both fluids unmixed; see figure 4)

No exact expression exists for this case, but the following is a very good approximation. Note that an iterative solution is required for AU.

$$E = 1 - e \left( e \left( -\frac{AU}{C_{\min}} \frac{C_{\min}}{C_{\max}} y \right) - 1 \right) \left( \frac{C_{\max}}{C_{\min}} \frac{1}{y} \right)$$

where:

$$y = \left[ \frac{C_{\min}}{AU} \right]^{0.22}$$

References:

W.M. Kays and A.L. London, *Compact Heat Exchangers*, National Press, 1955  
 Eckert and Drake, *Heat and Mass Transfer*, McGraw-Hill.

Remarks:

For cases where the inlet and outlet temperatures of one of the fluids are equal (change of phase), use zero for the heat capacity of that fluid.

The solution for AU in the crossflow configuration takes significantly longer than other solutions because of the iterative technique required.

The program must be allowed to solve for all values (AU, Q,  $T_{co}$ ,  $T_{ho}$ , and E). It is quite possible for the heat balance equations to yield physically meaningless solutions for a particular configuration. However, the message "2ND LAW ERR" will be displayed if the 2nd law of thermodynamics has been violated during the calculation of AU or Q.

This program is organized into five routines. The first routine performs heat balance calculations and acts as a controller for the four configuration subroutines. Each configuration subroutine has two sections that calculate AU and E for that heat exchanger. You should first load the controller, then load the configuration of interest as a separate program.

You may wish to write your own configuration routines. A routine for a configuration must be in the following format:

```

LBL ACON
  ●
  ●
  ●
(calculates AU for this configuration)
  ●
  ●
  ●
RTN
  ●
  ●
  ●
LBL ECON
  ●
  ●
  ●
(calculates E for this configuration)
  ●
  ●
  ●
END

```

Example:

A liquid at 168°F is to be cooled to 117°F. The liquid has a heat capacity of 0.42 Btu/LBM-°F and flows at 7700 LBM/hr. Cooling water (heat capacity = 1.00) is available at 4800 lbm/hr at 50°F. For counterflow, crossflow, parallel-counterflow, and parallel flow heat exchangers with overall coefficients of 55 Btu/hr-ft<sup>2</sup>-°F what areas are required?

Keystrokes: (SIZE ≥ 023)

Display:

[////] [FIX] 4

Load main routine and counterflow subroutine.

[XEQ] [ALPHA] HEATX [ALPHA]

TC IN=?

50 [R/S]

TH IN=?

168 [R/S]

MC=?

4800 [R/S]

MH=?

7700 [R/S]

CPC=?

1 [R/S]

CPH=?

.42 [R/S]

SELECT KEY: E AU Q TC TH

Since the temperature of the outgoing fluid is known, press the [E] key.

[E]

THO=?

117 [R/S]

E=0.4322

[R/S]\*

AU=2,198.7662

[R/S]\*

Q=164,933.9999

[R/S]\*

TCO=84.3612

[R/S]\*

SELECT KEY: E AU Q TC TH

Keystrokes:	Display:
Since $A = AU/U$ , calculate A.	
2198.7662 [ENTER] 55 [÷]	39.9776
Load crossflow subroutine.	
[XEQ] [ALPHA] HEATX [ALPHA]	TC IN=?
[R/S]	TH IN=?
[R/S]	MC=?
[R/S]	MH=?
[R/S]	CPC=?
[R/S]	CPH=?
[R/S]	SELECT KEY: E AU Q TC TH
[E]	THO=?
[R/S]	E=0.4322
[R/S]*	AU=2,353.6675
[R/S]*	Q=164,934.0000
[R/S]*	TCO=84.3613
[R/S]	SELECT KEY: E AU Q TC TH
2353.6675 [ENTER] 55 [÷]	42.7940

An analogous procedure will yield areas of  $42.2776 \text{ ft}^2$  and  $45.1494 \text{ ft}^2$  for parallel-counterflow and parallel exchanges respectively.

# User Instructions

				SIZE: 023
STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1.	Load program and then:		[GTO] ..	
2.	Load configuration subroutine corresponding			
	to your heat exchanger geometry		[XEQ] HEATX	TC IN=?
3.	Input inlet temperature of cold fluid	$T_{cin}$	[R/S]	TH IN=?
4.	Input inlet temperature of hot fluid	$T_{hin}$	[R/S]	MC=?
5.	Input mass flow rate of cold fluid	$m_c$	[R/S]	MH=?
6.	Input mass flow rate of hot fluid	$m_h$	[R/S]	CPC=?
7.	Input specific heat of cold fluid	$C_{pc}$	[R/S]	CPH=?
8.	Input specific heat of hot fluid	$C_{ph}$	[R/S]	SELECT KEY
				E AU Q TC TH
9.	Select the known value:			
	heat exchanger effectiveness		[A]	E=?
	area-heat transfer coefficient product		[B]	AU=?
	heat transfer		[C]	Q=?
	outlet temperature of cold fluid		[D]	TCO=?
	outlet temperature of hot fluid		[E]	THO=?
	input the known value.	E	[R/S]	
		AU	[R/S]	
		Q	[R/S]	
		TCO	[R/S]	
		THO	[R/S]	
	The four variables other than the one you			E=
	input will be output. The output order		[R/S]*	AU=
	will vary depending on which value was		[R/S]*	Q=
	input. If the 2nd law of thermodynamics		[R/S]*	TCO=
	is violated, the message "2ND LAW ERR"		[R/S]*	THO=
	will be displayed.		[R/S]*	SELECT KEY



# Program Listings

## Heat Exchanger - Main Routine

01 *LBL "HEA TX"	Input values.	49 XEQ "IN"	Input AU.
02 2		50 ADV	
03 STO 00		51 GTO 16	
04 "TC IN"		52 *LBL B	
05 XEQ "IN"		53 SF 03	
06 "TH IN"		54 10	
07 XEQ "IN"		55 STO 00	Input Q.
08 14		56 "AU"	
09 STO 00		57 XEQ "IN"	
10 "MC"		58 ADV	
11 XEQ "IN"		59 GTO 01	
12 "MH"		60 *LBL C	
13 XEQ "IN"		61 SF 04	Input TCO.
14 "CPC"		62 11	
15 XEQ "IN"		63 STO 00	
16 RCL 15		64 "Q"	
17 *		65 XEQ "IN"	
18 STO 05		66 ADV	
19 "CPH"		67 GTO 05	Input THO.
20 XEQ "IN"		68 *LBL D	
21 RCL 16		69 SF 05	
22 *		70 12	
23 STO 06		71 STO 00	
24 "CON"		72 "TCO"	
25 ASTO 22	73 XEQ "IN"	Calculate AU.	
26 *LBL 06	74 ADV		
27 CF 02	75 GTO 14		
28 CF 03	76 *LBL E		
29 CF 04	77 SF 06		
30 CF 05	78 13		
31 CF 06	79 STO 00	Calculate Q.	
32 CF 21	80 "THO"		
33 SF 27	81 XEQ "IN"		
34 "SELECT KEY: "	82 ADV		
35 AVIEW	83 GTO 04		
36 SF 21	84 *LBL 16		
37 PSE	85 FS?C 03		
38 *LBL 00	86 GTO 06		
39 ADV	87 RCL 10		
40 "E AU Q TC TH"	88 "A"		
41 PROMPT	89 XEQ 08		
42 GTO 00	90 STO 11		
43 *LBL A	91 "AU"		
44 SF 02	92 XEQ "O"		
45 9	93 *LBL 01		
46 STO 00	94 FS?C 04		
47 SF 01	95 GTO 06		
48 "E"	96 RCL 11		
	97 "E"		
	98 XEQ 08		
	99 RCL 07		

# Program Listings

## Heat Exchanger - Main Routine

100 *		151 X<>Y	
101 RCL 04		152 RCL 04	
102 RCL 03		153 RCL 03	
103 -		154 -	
104 *		155 /	
105 STO 12		156 RCL 05	
106 "0"		157 RCL 06	
107 XEQ "0"		158 X<=Y?	
108*LBL 05		159 X<>Y	
109 FS?C 05		160 RDN	
110 GTO 06	Calculate TCO.	161 X=0?	
111 RCL 12		162 X<> T	
112 RCL 05		163 /	
113 X#0?		164 STO 10	
114 /		165 SF 01	
115 RCL 03		166 "E"	
116 +		167 XEQ "0"	
117 STO 13		168 GTO 16	
118 "TCO"		169*LBL "A0"	
119 XEQ "0"		170 1	
120*LBL 14		171 RCL 10	
121 FS?C 06		172 -	
122 GTO 06	Calculate THO.	173 LN	
123 RCL 13		174 CHS	A0 for $C_{min}=0.00$ .
124 RCL 03		175 RTN	
125 -		176*LBL "E0"	
126 RCL 05		177 1	
127 *		178 RCL 11	
128 RCL 06		179 CHS	
129 X#0?		180 E↑X	E0 for $C_{min}=0.00$ .
130 /		181 -	
131 RCL 04		182 RTN	
132 -		183*LBL 08	
133 CHS		184 RCL 05	
134 STO 14		185 RCL 06	
135 "THO"		186 X>Y?	
136 XEQ "0"		187 X<>Y	
137*LBL 04		188 X<>Y	
138 FS?C 02		189 STO 07	
139 GTO 06		190 X<>Y	
140 RCL 13	Calculate E.	191 X#0?	
141 RCL 03		192 STO 07	
142 -		193 X<>Y	
143 RCL 05		194 X#0?	
144 *		195 /	
145 RCL 04		196 STO 09	
146 RCL 14		197 SF 25	
147 -		198 X=0?	
148 RCL 06		199 "H0"	
149 *		200 X#0?	
150 X=0?		201 ARCL 22	Find $C_{min}$ and execute configuration subroutine.

# Program Listings

202	ASTO T		51	
203	XEQ IND			
	T			
204	FS?C 25			
205	RTN			
206	"2ND LAW			
	ERR"	Trap errors from		
207	PROMPT	subroutines		
208	GTO 06			
209	*LBL "IN"			
210	CF 22	Input subroutine	60	
211	1			
212	ST+ 00			
213	RCL IND			
	00			
214	"F="			
215	ASTO Y			
216	"F?"			
217	CF 21			
218	AVIEW			
219	SF 21		70	
220	CLA			
221	ARCL Y			
222	STOP			
223	STO IND			
	00			
224	FS? 22			
225	FC? 55			
226	RTN			
227	ARCL X			
228	PRA			
229	RTN	Print if printer	80	
230	*LBL "O"	is attached		
231	"F="			
232	ARCL X	Output subroutine		
233	AVIEW			
234	.END.			
40			90	
50			00	



# Program Listings

## Parallel Flow Subroutine

01	LBL "ACO	Calculate AU.	51
N"			
02	RCL 09		
03	1		
04	+		
05	RCL 10		
06	*		
07	CHS		
08	1		
09	+		60
10	LN		
11	CHS		
12	1		
13	RCL 09		
14	+		
15	/		
16	RCL 07		
17	*		
18	RTN		
19	LBL "ECO	70	
N"			
20	1		
21	+		
22	RCL 11		
23	RCL 07		
24	/		
25	*		
26	CHS		
27	E↑X		
28	CHS	80	
29	1		
30	+		
31	1		
32	RCL 09		
33	+		
34	/		
35	RTN		
40			90
50			00

# Program Listings

## Counter Flow Subroutine

<p>01♦LBL "ACO N"</p>	<p>Calculate AU.</p>	<p>50 RCL 11 51 RCL 07 52 / 53 ENTER↑ 54 ENTER↑ 55 1 56 + 57 / 58 RTN</p>	60
02 RCL 10			
03 1/X			
04 -			
05 1			
06 LASTX			
07 -			
08 /			
09 LN			
10 1			
11 RCL 09			
12 -			
13 X=0?			
14 GTO 10			
15 /			
16 RCL 07			
17 *			
18 RTN			
19♦LBL 10			
20 RCL 10		70	
21 1			
22 RCL 10			
23 -			
24 /			
25 RCL 07			
26 *			
27 RTN			
28♦LBL "ECO			
N"			
29 1	80		
30 -			
31 RCL 11			
32 RCL 07			
33 /			
34 *			
35 E↑X			
36 1			
37 X<>Y			
38 -			
39 LASTX	90		
40 RCL 09			
41 *			
42 1			
43 X<>Y			
44 -			
45 X=0?			
46 GTO 11			
47 /			
48 RTN			
49♦LBL 11	00		

# Program Listings

## Parallel-Counter Flow Subroutine

01♦LBL "ACO N"	Calculate AU.	50♦LBL 12	
02 XEQ 12		51 RCL 09	
03 2		52 1	
04 *		53 +	
05 RCL 12		54 STO 08	
06 2		55 RCL 09	
07 RCL 10		56 X↑2	
08 /		57 1	
09 +		58 +	
10 RCL 08		59 SQRT	
11 -		60 STO 12	
12 /		61 RTN	
13 CHS			
14 1			
15 +			
16 LN			
17 RCL 12			
18 /			
19 CHS		70	
20 RCL 07			
21 /			
22 LASTX			
23 X↑2			
24 *			
25 RTN			
26♦LBL "ECO N"		Calculate E.	
27 XEQ 12			
28 RCL 11	80		
29 RCL 07			
30 /			
31 RCL 12			
32 *			
33 CHS			
34 E↑X			
35 1			
36 X<>Y			
37 +			
38 1			
39 LASTX	90		
40 -			
41 /			
42 RCL 12			
43 *			
44 RCL 08			
45 +			
46 2			
47 X<>Y			
48 /			
49 RTN	00		

# Program Listings

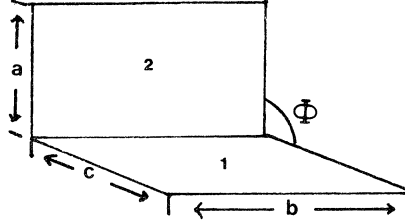
## Cross Flow Subroutine

<pre> 01♦LBL "ACO N" 02 0 03 STO 19 04 1 05 RCL 10 06 CHS 07 STO 21 08 + 09 LN 10 CHS 11 STO 11 12♦LBL 13 13 RCL 11 14 XEQ "ECO N" 15 RCL 10 16 - 17 STO 20 18 RCL 19 19 RCL 11 20 STO 19 21 - 22 RCL 21 23 RCL 20 24 STO 21 25 - 26 / 27 * 28 ST- 11 29 ABS 30 1 E-4 31 X&lt;=Y? 32 GTO 13 33 RCL 11 34 RTN 35♦LBL "ECO N" </pre>	<p>Calculate AU.</p>	<pre> 49 E↑X 50 1 51 - 52 * 53 E↑X 54 CHS 55 1 56 + </pre>
<pre> 36 RCL 11 37 RCL 07 38 / 39 ENTER↑ 40 ENTER↑ 41 .22 42 Y↑X 43 RCL 09 44 / 45 / 46 LASTX 47 X&lt;&gt;Y 48 CHS </pre>	<p>Calculate E.</p>	



## VIEW FACTOR

Given two surfaces, oriented as shown below, this program calculates the fraction of radiation leaving one surface that gets to the other, assuming a 90° angle.



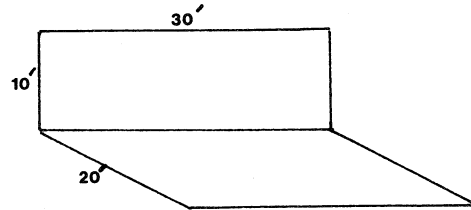
The fraction of radiation that gets from 1 to 2 is the same as that which gets from 2 to 1.

Equations:

$$\begin{aligned}
 X &= a/b, \quad Y = c/b, \quad Z = X^2 + Y^2 - 2XY \cos \Phi \\
 F_{A_1 - A_2}(\pi Y) &= -\frac{\sin 2\Phi}{4} \left[ XY \sin \Phi + \left( \frac{\pi}{2} - \Phi \right) (X^2 + Y^2) \right. \\
 &\quad + Y^2 \tan^{-1} \left( \frac{X - Y \cos \Phi}{Y \sin \Phi} \right) \\
 &\quad \left. + X^2 \tan^{-1} \left( \frac{Y - X \cos \Phi}{X \sin \Phi} \right) \right] \\
 &\quad + \frac{\sin^2 \Phi}{4} \left\{ \left( \frac{2}{\sin^2 \Phi} - 1 \right) \ln \left[ \frac{(1 + X^2)(1 + Y^2)}{1 + Z} \right] \right. \\
 &\quad \left. + Y^2 \ln \left[ \frac{Y^2(1 + Z)}{(1 + Y^2)Z} \right] + X^2 \ln \left[ \frac{X^2(1 + X^2) \cos 2\Phi}{Z(1 + Z) \cos 2\Phi} \right] \right\} \\
 &\quad + Y \tan^{-1} \left( \frac{1}{Y} \right) + X \tan^{-1} \left( \frac{1}{X} \right) - \sqrt{Z} \tan^{-1} \left( \frac{1}{\sqrt{Z}} \right) \\
 &\quad + \frac{\sin \Phi \sin 2\Phi}{2} X \sqrt{1 + X^2 \sin^2 \Phi} \\
 &\quad \times \left[ \tan^{-1} \left( \frac{X \cos \Phi}{\sqrt{1 + X^2 \sin^2 \Phi}} \right) \right. \\
 &\quad \left. + \tan^{-1} \left( \frac{Y - X \cos \Phi}{\sqrt{1 + X^2 \sin^2 \Phi}} \right) \right] \\
 &\quad + \cos \Phi \int_0^Y \sqrt{1 + \xi^2 \sin^2 \Phi} \left[ \tan^{-1} \left( \frac{X - \xi \cos \Phi}{\sqrt{1 + \xi^2 \sin^2 \Phi}} \right) \right. \\
 &\quad \left. + \tan^{-1} \left( \frac{\xi \cos \Phi}{\sqrt{1 + \xi^2 \sin^2 \Phi}} \right) \right] d\xi
 \end{aligned}$$

Example:

Find the view factor for the arrangement below:



Keystrokes:

```
[XEQ] [ALPHA] SIZE [ALPHA] 006
[XEQ] [ALPHA] VIEW [ALPHA]
30 [R/S]
10 [R/S]
20 [R/S]
```

Display:

```
WIDTH ?
HEIGHT ?
DEPTH ?
F=0.1595
```

(what if the height were only 8'?)

```
[A]
[R/S]
8 [R/S]
[R/S]
```

```
WIDTH ?
HEIGHT ?
DEPTH ?
F=0.1379
```





# Program Listings

01*LBL "VIE W"	Initialize	48 *	
02 SF 27	-----	49 RCL 04	
03*LBL A	Input	50 X↑2	
04 CF 22		51 1	
05 "WIDTH ?		52 +	
"		53 /	
06 PROMPT		54 RCL 05	
07 FS?C 22		55 /	
08 STO 00		56 LN	
09 "HEIGHT		57 RCL 04	
?"		58 X↑2	
10 PROMPT		59 *	
11 FS?C 22		60 +	
12 STO 01		61 RCL 03	
13 "DEPTH ?		62 X↑2	
"		63 RCL 05	
14 PROMPT		64 1	
15 FS?C 22		65 +	
16 STO 02		66 *	
17 RCL 01	Calculate	67 RCL 03	
18 RCL 00	X, Y and Z	68 X↑2	
19 /	-----	69 1	
20 STO 03		70 +	
21 X↑2		71 /	
22 RCL 02		72 RCL 05	
23 RCL 00		73 /	
24 /		74 LN	
25 STO 04		75 RCL 03	
26 X↑2		76 X↑2	
27 +		77 *	
28 STO 05		78 +	
29 RCL 03	Calculate	79 4	
30 X↑2	F	80 /	
31 1		81 1	
32 +		82 ASIN	
33 RCL 04		83 2	
34 X↑2		84 *	
35 1		85 PI	
36 +		86 /	
37 *		87 *	
38 RCL 05		88 RCL 03	
39 1		89 1/X	
40 +		90 ATAN	
41 /		91 RCL 03	
42 LN		92 *	
43 RCL 04		93 +	
44 X↑2		94 RCL 04	
45 RCL 05		95 1/X	
46 1		96 ATAN	
47 +		97 RCL 04	
		98 *	





## HEAT TRANSFER THROUGH COMPOSITE CYLINDERS AND WALLS

This program can be used to calculate the overall heat transfer coefficient for composite tubes and walls from individual section conductances and surface coefficients.

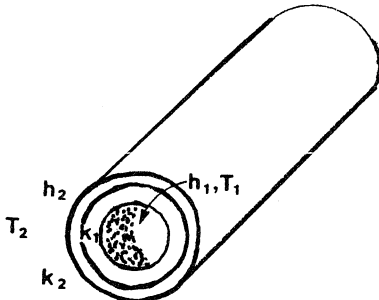


Figure 1.—Composite tube

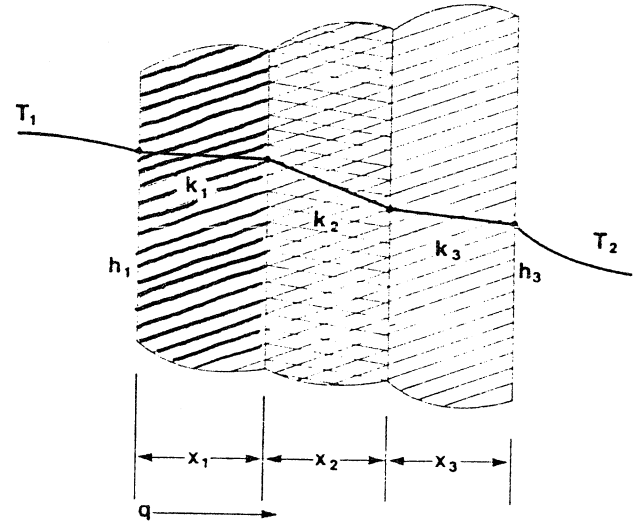


Figure 2.—Composite wall

Equations:

The overall heat transfer coefficient  $U$  is defined by:

$$q/L = U \Delta T$$

or

$$q/A = U \Delta T$$

where  $\Delta T$  is the total temperature difference ( $T_2 - T_1$ ),  $q/L$  is the heat transfer per unit length of pipe, and  $q/A$  is the heat transfer per unit area of wall.

For cylinders

$$U = \frac{2\pi}{\frac{2}{h_1 D_1} + \frac{\ln(D_2/D_1)}{k_1} + \frac{\ln(D_3/D_2)}{k_2} + \dots + \frac{\ln(D_n/D_{n-1})}{k_{n-1}} + \frac{2}{h_n D_n}}$$

For walls

$$U = \frac{1}{\frac{1}{h_1} + \frac{x_1}{k_1} + \frac{x_2}{k_2} + \dots + \frac{x_n}{k_n} + \frac{1}{h_n}}$$

where

- h is the convective surface coefficient;
- $D_n$  is the outside diameter of the annulus;
- k is the conductive coefficient;
- x is the thickness of a wall section.

Remarks:

These equations are for steady state heat transfer through materials with constant properties in all directions.

For composite cylinders, inputs must start with the inside convective coefficient and work out.

Zero is an invalid input for D, k, and h.

Dimensional consistency must be maintained.

Example:

A steel pipe with an inside diameter of 4 inches and a thickness of 0.5 inches has a conductivity of 25 Btu/ft-hr-°F. Two inches of asbestos (k = 0.1 Btu/hr-ft-°F) enclose the pipe bringing the total diameter to 9 inches. If the inside convective coefficient is 1000 Btu/hr-ft<sup>2</sup>-°F and the outside coefficient is 5 Btu/hr-ft<sup>2</sup>-°F, what is the overall heat transfer coefficient? What is the heat loss for 100 feet of pipe if ΔT is 115°F?

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 009

[XEQ] [ALPHA] CYL [ALPHA]

NO. OF SECTS?

2 [R/S]

D?

4 [ENTER↑] 12 [÷] [R/S]

H?

1000 [R/S]

D?

5 [ENTER↑] 12 [÷] [R/S]

K?

25 [R/S]

D?

9 [ENTER↑] 12 [÷] [R/S]

K?

0.1 [R/S]

H?

5 [R/S]

U=0.98 Btu/hr-ft-°F

115 [X]

112.44 Btu/hr-ft

100 [X]

11,244.20 Btu/hr

# User Instructions

SIZE: 009

STEP	INSTRUCTIONS	INPUT	FUNCTION	DISPLAY
1	Load program			
2	For walls go to step 3, and for cylinders go to step 9.			
3	Initialize for walls		[XEQ] WALLS	NO. OF SECTS?
4	Key in number of sections	N	[R/S]	H?
5	Key in the first section's convective coefficient	$h_1$	[R/S]	X?
6	Key in thickness of the current section	$x_i$	[R/S]	k?
7	Key in the conductive coefficient for the section of step 6 (Repeat steps 6 and 7 for each section. The prompt after the last section will be "H?")	$k_i$	[R/S]	X? or H?
8	Key in the last section's convective coefficient	$h_n$	[R/S]	U=
9	Initialize for cylinders		[XEQ] CYL	NO. OF SECTS?
10	Key in number of sections	N	[R/S]	D?
11	Key in the inside section's inner diameter	$D_1$	[R/S]	H?
12	Key in the inside convective coefficient	$h_1$	[R/S]	D?
13	Key in the outside diameter of the current section	$D_i$	[R/S]	K?
14	Key in the conductive coefficient for the section of step 13 (Repeat steps 13 and 14 for each section)	$k_i$	[R/S]	D? or H?
15	Key in the outside convective coefficient	$h_n$	[R/S]	U=

# Program Listings

<pre> 01*LBL "CYL " 02 SF 00 03 GTO 00 04*LBL "WAL LS" 05 CF 00 06*LBL 00 07 FIX 2 08 1 09 FS? 00 10 PI 11 STO 06 12 CLX 13 STO 08 14 FC? 00 15 GTO 01 16 "NO. OF SECTS?" 17 PROMPT 18 STO 00 19 "D?" 20 PROMPT 21*LBL A 22 STO 07 23 "H?" 24 PROMPT 25 * 26 1/X 27 ST+ 08 28 FC?C 00 29 GTO "U" 30*LBL B 31 "D?" 32 PROMPT 33 STO 01 34 "K?" 35 PROMPT 36 1/X 37 X&lt;&gt;Y 38 RCL 07 39 X&lt;&gt;Y 40 STO 07 41 / 42 LN 43 * 44 2 45 / 46 ST- 08 47 DSE 00 48 GTO B </pre>	<p>Initialization</p> <hr/> <p>Cylinders</p>	<pre> 49 RCL 01 50 GTO A 51*LBL 01 52 SF 00 53 "NO. OF SECTS?" 54 PROMPT 55 STO 00 56*LBL C 57 "H?" 58 PROMPT 59 1/X 60 ST+ 08 61 FC?C 00 62 GTO "U" 63*LBL D 64 "X?" 65 PROMPT 66 "K?" 67 PROMPT 68 / 69 ST+ 08 70 DSE 00 71 GTO D 72 GTO C 73*LBL "U" 74 RCL 08 75 1/X 76 RCL 06 77 * 78 STO 04 79 "U=" 80 ARCL X 81 AVIEW 82 STOP 83 .END. </pre>	<hr/> <p>Walls</p> <hr/> <p>Calculate U and display</p>
		90	
		00	

# 48 REGISTERS, STATUS, FLAGS, ASSIGNMENTS

DATA REGISTERS			STATUS				
00	No. of surfaces outside diameter	50	SIZE	009	TOT. REG.	034	USER MODE
			ENG		FIX	2	SCI
			DEG		RAD		GRAD
	U						ON
							OFF
							X
05	l or $\pi$ temp. storage $\Sigma R$	55	FLAGS				
			#	INIT S/C	SET INDICATES	CLEAR INDICATES	
			00		Cyl	Walls	
10		60					
15		65					
20		70					
25		75					
30		80					
35		85					
			ASSIGNMENTS				
			FUNCTION	KEY	FUNCTION	KEY	
40		90					
45		95					



## BLACK BODY THERMAL RADIATION

Bodies with finite temperatures emit thermal radiation. The higher the absolute temperature, the more thermal radiation emitted. Bodies which emit the maximum possible amount of energy at every wavelength for a specified temperature are said to be black bodies. While black bodies do not actually exist in nature, many surfaces may be assumed to be black for engineering considerations.

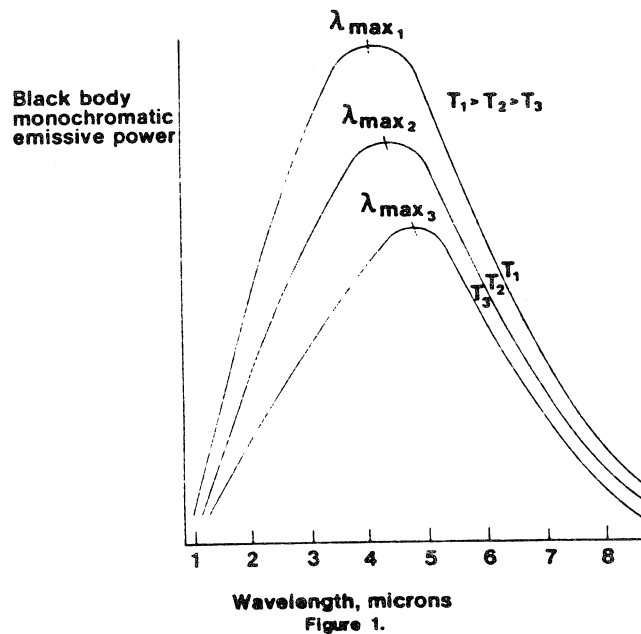


Figure 1.

### Notes:

A half minute or more may be required to obtain  $E_b(0-\lambda)$  or  $E_b(\lambda_1-\lambda_2)$  since the integration is numerical.

Sources differ on values for constants. This could yield small discrepancies between published tables and program outputs.

Figure 1 is a representation of black body thermal emission as a function of wavelength. Note that as temperature increases, the area under the curves (total emissive power  $E_b(0-\infty)$ ) increases. Also note that the wavelength of maximum emissive power  $\lambda_{max}$  shifts to the left as temperature increases.

This program calculates the wavelength of maximum emissive power for a given temperature, the temperature for which a given wavelength would be the wavelength of maximum emissive power, the total emissive power over all wavelengths, the emissive power at a particular wavelength, the emissive power from zero to a specified wavelength, and the emissive power between specified wavelengths.

Equations:

$$\lambda_{\max} T_{\lambda_{\max}} = c_3$$

$$E_{b(0-\infty)} = \sigma T^4$$

$$E_{b\lambda} = \frac{2\pi c_1}{\lambda^5 (e^{c_2/\lambda T} - 1)}$$

$$\begin{aligned} E_{b(0-\lambda)} &= \int_0^\lambda E_{b\lambda} d\lambda \\ &= 2\pi c_1 \sum_{k=1}^{\infty} -T/kc_2 e^{-\frac{kc_2}{T\lambda}} \left[ \left( \frac{1}{\lambda} \right)^3 + \frac{3T}{\lambda^2 kc_2} \right. \\ &\quad \left. + \frac{6}{\lambda} \left( \frac{T}{kc_2} \right)^2 + 6 \left( \frac{T}{kc_2} \right)^3 \right] \end{aligned}$$

$$E_{b(\lambda_1 - \lambda_2)} = E_{b(0-\lambda_2)} - E_{b(0-\lambda_1)}$$

where:

$\lambda_{\max}$  is the wavelength of maximum emissivity in microns;

T is the absolute temperature in °R or K;

$E_{b(0-\infty)}$  is the total emissive power in Btu/hr-ft<sup>2</sup> or Watts/cm<sup>2</sup>;

$E_{b\lambda}$  is the emissive power at  $\lambda$  in Btu/hr-ft<sup>2</sup>- $\mu$ m or Watts/cm<sup>2</sup>- $\mu$ m;

$E_{b(0-\lambda)}$  is the emissive power for wavelengths less than  $\lambda$  in Btu/hr-ft<sup>2</sup> or Watts/cm<sup>2</sup>;

$E_{b(\lambda_1 - \lambda_2)}$  is the emissive power for wavelengths between  $\lambda_1$  and  $\lambda_2$  in Btu/hr-ft<sup>2</sup> or Watts/cm<sup>2</sup>.

$$\begin{aligned} c_1 &= 1.8887982 \times 10^7 \text{ Btu}\cdot\mu\text{m}^4/\text{hr}\cdot\text{ft}^2 \\ &= 5.9544 \times 10^3 \text{ W}\mu\text{m}^4/\text{cm}^2 \end{aligned}$$

$$c_2 = 2.58984 \times 10^4 \mu\text{m}\cdot^\circ\text{R} = 1.4388 \times 10^4 \mu\text{m}\cdot\text{K}$$

$$c_3 = 5.216 \times 10^3 \mu\text{m}\cdot^\circ\text{R} = 2.8978 \times 10^3 \mu\text{m}\cdot\text{K}$$

$$\sigma = 1.713 \times 10^{-9} \text{ Btu/hr}\cdot\text{ft}^2\cdot^\circ\text{R}^4 = 5.6693 \times 10^{-12} \text{ W/cm}^2\cdot\text{K}^4$$

$$\sigma_{\text{exp}} = 1.731 \times 10^{-9} \text{ Btu/hr}\cdot\text{ft}^2\cdot^\circ\text{R}^4 = 5.729 \times 10^{-12} \text{ W/cm}^2\cdot\text{K}^4$$

References: HP-67/97 Users' Library Program.

Example:

What percentage of the radiant output of a lamp is in the visible range (0.4 to 0.7 microns) if the filament of the lamp is assumed to be a black body at 2400K?

Keystrokes: (SIZE  $\geq$  009)

[USER]  
 [XEQ] [ALPHA] BB [ALPHA]  
 SI [R/S]  
 2400 [R/S]  
 .4 [R/S]  
 [F]  
 .7 [R/S]  
 [C]  
 [÷]  
 100 [x]

Display:

(set USER mode)  
 UNITS?  
 TEMP?  
 WAVELENGTH?  
 SOLVE  
 WV LNTH 2?  
 EbL-L=4.9679  
 EbTOT=188.094  
 0.0264  
 2.6412



# Program Listings

01*LBL "BB"	Initialize and prompt for units	47 RCL 06	Calculate T( $\lambda_{max}$ )
02 CLRG		48 /	
03 CF 22		49 "TEMP="	
04 "UNITS?"		50 ARCL X	
05 AON		51 PROMPT	
06 PROMPT		52*LBL C	Calculate $E_b$ total
07 AOFF		53 RCL 05	
08 ASTO X		54 X↑2	
09 GTO IND		55 X↑2	
X		56 RCL 04	
10*LBL "SI"	Store units	57 *	
11 5954.4		58 "EbTOT="	
12 STO 01		59 ARCL X	
13 14388		60 PROMPT	
14 STO 02		61*LBL D	Calculate $E_{b\lambda}$
15 2897.8		62 RCL 01	
16 STO 03		63 ENTER↑	
17 5.6693 E		64 +	
-12		65 PI	
18 STO 04		66 *	
19 GTO 00		67 RCL 06	
20*LBL "EN"		68 5	
21 18887982		69 Y↑X	
22 STO 01		70 /	
23 25998.4		71 RCL 02	
24 STO 02		72 RCL 06	
25 5216		73 /	
26 STO 03		74 RCL 05	
27 .171312		75 /	
E-08		76 E↑X	
28 STO 04		77 1	
29*LBL 00	Input prompting	78 -	
30 "TEMP?"		79 /	
31 PROMPT		80 "EbL="	
32 STO 05		81 ARCL X	
33 "WAVELEN		82 PROMPT	
GTH?"		83*LBL E	Calculate $E_b(0-\lambda)$
34 PROMPT		84 0	
35 STO 06		85 STO 08	
36 "SOLVE"		86 STO 07	
37 PROMPT		87*LBL 01	
38*LBL A	Calculate $\lambda_{max}$	88 RDN	
39 RCL 03		89 CLX	
40 RCL 05		90 RCL 08	
41 /		91 RCL 02	
42 "WL MAX="		92 RCL 05	
"		93 /	
43 ARCL X		94 -	
44 PROMPT		95 STO 08	
45*LBL B		96 3	
46 RCL 03		97 X<>Y	





## ECONOMIC BREAK EVEN FOR SOLAR EQUIPMENT

This program calculates the number of years necessary for solar equipment to pay for itself.

Equation:

$$\text{YEARS} = \frac{-\ln \left\{ 1 - \frac{\$ \text{ SPENT } (\% \text{INT} - \% \text{INF})}{365 (\text{BTU}/\text{DAY}) (\$/\text{BTU})} \right\}}{\ln \left\{ 1 + \frac{\% \text{INT} - \% \text{INF}}{1 + \% \text{INF}} \right\}}$$

where:

- \$ SPENT = the cost of the solar equipment.
- \$/BTU = the cost of purchased energy per BTU.
- BTU/DAY = the amount of energy drawn from your solar equipment per day.
- %INT = the current lending rate to buy equipment
- %INF = the expected inflation rate for the cost of energy.
- YEARS = the number of years before the solar equipment pays for itself.

Example:

Aaron B. Waters wants to buy \$2000 worth of solar equipment with which he hopes to bring in 75,000 BTU per day. The cost per BTU for the energy source he is replacing is  $3.66 \times 10^{-6}$  \$/BTU. The lending rate is 14.5% and the inflation rate is 15%. How long will it take the equipment to pay for itself?

Keystrokes:

Display:

[XEQ] [ALPHA] SIZE [ALPHA] 005

[XEQ] [ALPHA] EBE [ALPHA]

\$ SPENT ?

2000 [R/S]

\$/BTU ?

3.66 [EEX] 6 [CHS] [R/S]

BTU/DAY ?

75000 [R/S]

%INT ?

14.5 [R/S]

%INF ?

15 [R/S]

21.83 YEARS



What if he spent \$1500 and got 65,000 BTU/DAY?

[A]	\$ SPENT ?
1500 [R/S]	\$/BTU ?
[R/S]	BTU/DAY ?
65000 [R/S]	%INT ?
[R/S]	%INF ?
[R/S]	19.01 YEARS







## SOLAR PANEL ARRAY

When solar panels are installed on flat roofs or on the ground it often is necessary or desirable to arrange the collectors in several rows, one in back of another. In such an array the arrangement to prevent the south-most rows from shading the others becomes important. This program calculates the appropriate distance between the collector arrays. Input is the Date, Latitude, Longitude, Time of Day, Local Standard Time Meridian, and the length of the solar collector panel.

Actual distance between rows, will, in final analysis, be a matter of judgment based on available space and economic conditions. For example, partial shading during the early morning and late afternoon hours in late December may be an acceptable compromise based on limited space available for panel mounting.

A most important factor in establishing the array is to establish the sun angle,  $S$ , and shade length,  $D_2$ , on an hourly and daily basis. Assuming that the array is facing south, and that you know the latitude of the location, this can be accomplished for any day of the year and time of day.

### Equations:

$$N = [\text{INT}(365.25y') + \text{INT}(30.6001m') + DD + 1,720,983] - \\ [\text{INT}(365.25(\text{YYYY}-1)) + \text{INT}(30.6001(\text{MM}+13)) + 1,720,983]$$

Where:

$N$ =Numbered day of the year counting from Jan. 1 as day 1

$MM$ =Month

$DD$ =Day of the month

$YYYY$ =Year

$y'$  = Year-1, if  $MM=1$  or  $2$   
Year, if  $MM > 2$

$m'$  = Month+13, if  $MM=1$  or  $2$   
Month +1, if  $MM > 2$

$$\delta = 23.45 \text{SIN} \left[ \frac{360(284+N)}{365} \right]$$

Where:

$\delta$  = Sun's declination, degrees

$$AST = LST + 4(LSM - LON)$$

Where: LON = Local Longitude

AST = Apparent Solar Time

LST = Local Standard Time

LSM = Local Standard Meridian

$$S = \text{TAN}^{-1} \frac{\text{SIN } \delta \text{ SIN } \phi + \text{COS } \delta \text{ COS } \phi \text{ COS } w}{\text{COS } \delta \text{ SIN } \phi \text{ COS } w - \text{SIN } \delta \text{ COS } \phi}$$

Where:

S = sun angle in a plane perpendicular to the earth and parallel to the longitude

$\phi$  = latitude (north positive)

w = hour angle, solar noon being zero, and each hour equaling  $15^\circ$  of longitude with morning positive and afternoon negative

$$V = L \text{ SIN } T$$

$$D_1 = \frac{V}{\text{TAN } S} + L \text{ COS } T$$

$$D_2 = \frac{V}{\text{TAN } S}$$

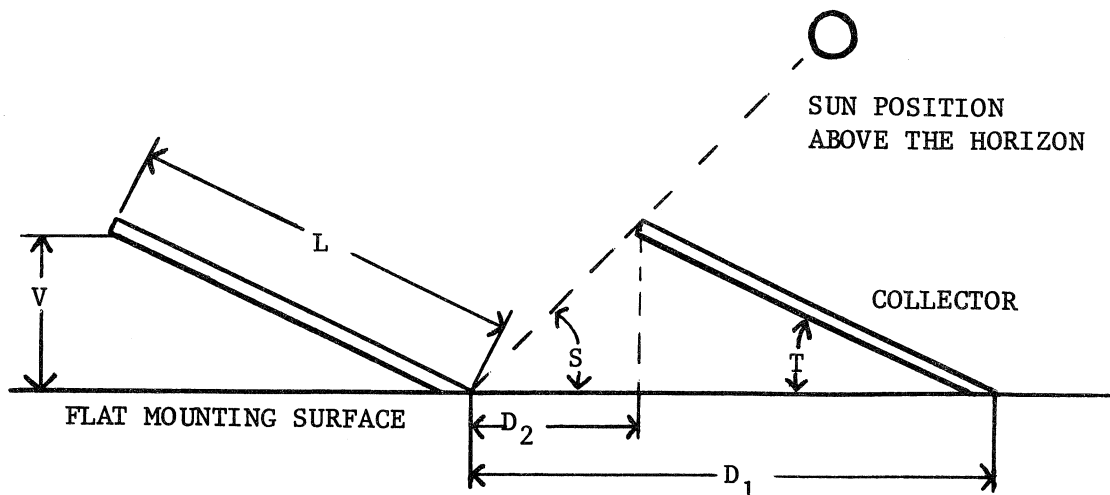
Where:

V = height from the horizontal to the top of solar panel, FT.

$D_1$  = distance from front of first row of collectors to the front of the row behind, FT.

$D_2$  = shade length, FT.

L = solar collector panel length, FT.



Establishing Distance Between Rows on a Flat Mounting Surface

## Example:

In an array of 7' panels located at 36°25' north latitude and 97°30' west longitude with a panel tilt of 46° find V, D<sub>1</sub> and D<sub>2</sub> at 12 noon Central Standard Time on 12/21/1979.

## Keystrokes:

[XEQ] [ALPHA] SIZE [ALPHA] 012

[XEQ] [ALPHA] PANEL [ALPHA]

12.211979 [R/S]

36.25 [R/S]

97.3 [R/S]

12 [R/S]

90 [R/S]

46 [R/S]

7 [R/S]

[R/S]

[R/S]

What about at 1 PM on 6/1/1979?

[A]

6.011979 [R/S]

[R/S]

[R/S]

13 [R/S]

[R/S]

[R/S]

[R/S]

[R/S]

[R/S]

## Display:

MM.DDYyyy?

LAT ?

LONG ?

TIME ?

TIME MER ?

TILT  $\Delta$  ?

LENGTH ?

V=5.0354

D<sub>1</sub>=13.6006

D<sub>2</sub>=8.7380

MM.DDYyyy?

LAT ?

LONG ?

TIME ?

TIME MER ?

TILT  $\Delta$  ?

LENGTH ?

V = 5.0354

D<sub>1</sub> = 6.1373

D<sub>2</sub> = 1.2747





# Program Listings

<pre> 01♦LBL "PAN EL" 02 SF 27 03♦LBL A 04 CF 22 05 "MM.DDYY YY?" 06 PROMPT 07 FC?C 22 08 GTO 04 09 STO 00 10 ENTER↑ 11 INT 12 STO 07 13 - 14 1 E2 15 * 16 ENTER↑ 17 INT 18 STO 08 19 - 20 1 E4 21 * 22 STO 09 23 CF 02 24♦LBL 01 25 2 26 RCL 07 27 X&gt;Y? 28 GTO 00 29 RCL 09 30 1 31 - 32 STO 09 33 RCL 07 34 13 35 + 36 STO 07 37 GTO 03 38♦LBL 00 39 RCL 07 40 1 41 + 42 STO 07 43♦LBL 03 44 365.25 45 RCL 09 46 * 47 INT 48 30.6001 49 RCL 07                     </pre>	<pre> Initialization ----- Input ----- Calculate DOY and declination                     </pre>	<pre> 50 * 51 INT 52 + 53 RCL 08 54 + 55 1720982 56 + 57 FS? 02 58 GTO 02 59 STO 01 60 1 61 STO 07 62 STO 08 63 SF 02 64 GTO 01 65♦LBL 02 66 RCL 01 67 1 68 + 69 X&lt;&gt;Y 70 - 71 STO 09 72 RCL 00 73 CF 02 74 360 75 ENTER↑ 76 284 77 RCL 09 78 + 79 365 80 / 81 * 82 SIN 83 23.45 84 * 85 STO 08 86♦LBL 04 87 "LAT ?" 88 PROMPT 89 HR 90 FS?C 22 91 STO 05 92 "LONG ?" 93 PROMPT 94 HR 95 FS?C 22 96 STO 02 97 "TIME ?" 98 PROMPT 99 HR 100 FS?C 22                     </pre>	<pre> Day # Get Day # for Jan. 1  DOY  Declination                     </pre>
--	---	--	---





## CONDUIT FLOW

This program solves for the average velocity, or the pressure drop for viscous, incompressible flow in conduits.

Equations:

$$v^2 = \frac{\Delta P / \rho}{2 \left( f \frac{L}{D} + \frac{K_T}{4} \right)}$$

For laminar flow ( $Re < 2300$ )

$$f = 16/Re.$$

For turbulent flow ( $Re > 2300$ )

$$\frac{1}{\sqrt{f}} = 1.737 \ln \frac{D}{\epsilon} + 2.28 - 1.737 \ln \left( 4.67 \frac{D}{\epsilon Re \sqrt{f}} + 1 \right)$$

is solved by Newton's method.

$$\frac{1}{\sqrt{f_0}} = 1.737 \ln \frac{D}{\epsilon} + 2.28$$

is used as an initial guess in the iteration.

where:  $Re$  is the Reynolds number, defined as  $\rho Dv/\mu$ ;

$D$  is the pipe diameter;

$\epsilon$  is the dimension of irregularities in the conduit surface (see table 1);

$f$  is the Fanning friction factor for conduit flow;

$\Delta P$  is the pressure drop along the conduit;

$\rho$  is the density of the fluid;

$\mu$  is the viscosity of the fluid;

$\nu$  is the kinematic viscosity of the fluid and  $\mu = \rho\nu$ ;

$L$  is the conduit length;

$v$  is the average fluid velocity;

$K_T$  is the total of the applicable fitting coefficients in table 1.

Table 1  
Fitting Coefficients

Fitting	K
Globe valve, wide open	7.5—10
Angle valve, wide open	3.8
Gate valve, wide open	0.15—0.19
Gate valve, 3/4 open	0.85
Gate valve, 1/2 open	4.4
Gate valve, 1/4 open	20
90° elbow	0.4—0.9
Standard 45° elbow	0.35—0.42
Tee, through side outlet	1.5
Tee, straight through	.4
180° bend	1.6
Entrance to circular pipe	0.25—0.50
Sudden expansion	$(1-A_{up}/A_{dn})^{2*}$
Acceleration from $v=0$ to $v=v_{entrance}$	1.0

\* $A_{up}$  is the upstream area and  $A_{dn}$  is the downstream area.

Table 2  
Surface Irregularities

Material	$\epsilon$ (feet)	$\epsilon$ (meters)
Drawn or Smooth Tubing	$5.0 \times 10^{-6}$	$1.5 \times 10^{-6}$
Commercial Steel or Wrought Iron	$1.5 \times 10^{-4}$	$4.6 \times 10^{-5}$
Asphalted Cast Iron	$4.0 \times 10^{-4}$	$1.2 \times 10^{-4}$
Galvanized Iron	$5.0 \times 10^{-4}$	$1.5 \times 10^{-4}$
Cast Iron	$8.3 \times 10^{-4}$	$2.5 \times 10^{-4}$
Wood Stave	$6.0 \times 10^{-4}$ to $3.0 \times 10^{-3}$	$1.8 \times 10^{-4}$ to $9.1 \times 10^{-4}$
Concrete	$1.0 \times 10^{-3}$ to $1.0 \times 10^{-2}$	$3.0 \times 10^{-4}$ to $3.0 \times 10^{-3}$
Riveted Steel	$3.0 \times 10^{-3}$ to $3.0 \times 10^{-2}$	$9.1 \times 10^{-4}$ to $9.1 \times 10^{-3}$

Reference:

Welty, Wicks, Wilson, *Fundamentals of Momentum, Heat and Mass Transfer*, John Wiley and Sons, Inc., 1969.

## Remarks:

The correlation gives meaningless results in the region  $2300 < Re < 4000$ .

The solution requires an iterative procedure. The time for solution will range from 10 seconds for  $\Delta P$ , to several minutes for  $v$ . The display setting is used to determine when the solution for  $v$  is adequately accurate. Time for solution of  $v$  is roughly proportional to the number or significant digits in the display setting.

If the conduit is not circular, an equivalent diameter may be calculated using the formula below:

$$D_{eq} = 4 \frac{\text{cross sectional area}}{\text{wetted perimeter}}$$

Unitary consistency must be maintained.

## Example:

A heat exchanger has 20, 3 meter tube passes (60 m of pipe) with 180 degrees bends connecting each pair of tubes (from table 1,  $K_T = 10 \times 1.6$ ). The fluid is water ( $\nu = 9.3 \times 10^{-7} \text{m}^2/\text{s}$ ,  $\rho = 10^3 \text{kg/m}^3$ ). The surface roughness is  $3 \times 10^{-4} \text{m}$  and the diameter is  $2.54 \times 10^{-2} \text{m}$ . If the fluid velocity is 3.05 m/s, what is the pressure loss? What is the Reynolds number? What is the Fanning friction factor?

## Keystrokes:

[XEQ] [ALPHA] SIZE [ALPHA] 015

[////] [ENG] 3

[XEQ] [ALPHA] CONDUIT [ALPHA]

9.3 [EEX] [CHS] 7 [ENTER↑]

[EEX] 3 [X] [R/S]

[EEX] 3 [R/S]

3 [EEX] [CHS] 4 [R/S]

60 [R/S]

2.54 [EEX] [CHS] 2 [R/S]

16 [R/S]

3.05 [R/S]

[R/S]

[R/S]

[R/S]

## Display:

U=?

RHO=?

E=?

L=?

D=?

KT=?

V=?

DP=?

DP=521.9E3

Re=83.30E3

F=10.18E-3



# Program Listings

01*LBL "CON DUIT"		51 X<>Y	
02 "U=?"		52 X*Y?	
03 PROMPT		53 GTO 03	
04 STO 09		54 "V="	
05 "RHO=?"	Input	55 RCL 02	
06 PROMPT		56 GTO 10	
07 STO 10		57*LBL 09	
08 ST/ 09		58 RCL 10	
09 "E=?"		59 RCL 13	
10 PROMPT		60 RCL 14	
11 STO 14		61 /	
12 "L=?"		62 STO 06	
13 PROMPT		63 LN	
14 STO 03		64 1.737	
15 "D=?"		65 STO 07	
16 PROMPT		66 *	
17 STO 13		67 2.28	
18 "KT=?"		68 +	
19 PROMPT		69 STO 12	
20 4		70 STO 05	
21 /		71 FS? 00	
22 STO 08		72 GTO 07	
23*LBL "CHA NGE"		73*LBL 08	
24 CF 22		74 16	
25 "V=?"		75 RCL 02	
26 PROMPT		76 RCL 13	
27 SF 00		77 *	
28 FS? 22		78 RCL 09	
29 CF 00		79 /	
30 STO 02		80 STO 01	
31 "DP=?"		81 2300	
32 PROMPT		82 X<=Y?	
33 STO 04		83 GTO 02	
34 XEQ 09	1st V	84 RDN	
35 FS? 00		85 /	
36 GTO 03		86 SQRT	
37 RCL 02		87 1/X	
38 X↑2		88 STO 05	
39 *	Calculate ΔP	89 GTO 07	
40 RCL 10		90*LBL 02	
41 *		91 RCL 12	
42 STO 04		92 RCL 05	
43 "DP="		93 -	
44 GTO 10		94 4.67	
45*LBL 03		95 RCL 06	
46 RND		96 *	
47 STO 00	Iterate to find V using 1st V as guess	97 RCL 01	
48 XEQ 08		98 /	
49 RND		99 RCL 05	
50 RCL 00		100 *	
		101 1	
		102 +	
			Calculate constants
			Is flow turbulent?
			Iterate to find $\frac{1}{\sqrt{f}}$



# Program Listings

103 STO 11		155 ARCL 01	
104 LN		156 PROMPT	
105 RCL 07		157 "F="	
106 *		158 RCL 05	
107 -		159 1/X	
108 RCL 11		160 X↑2	
109 1/X		161 ARCL X	
110 CHS		162 PROMPT	
111 1		163 RTN	
112 +		164 .END.	
113 RCL 07		uu	
114 *			
115 RCL 05			
116 /			
117 1			
118 +			
119 /			
120 ST+ 05			
121 RCL 05			
122 /			
123 ABS		70	
124 E-3			
125 X<=Y?			
126 GTO 02			
127 *LBL 07			
128 RCL 05			
129 1/X			
130 X↑2			
131 RCL 03			
132 *			
133 RCL 13		80	
134 /			
135 RCL 08			
136 +			
137 2			
138 *			
139 RCL 04			
140 RCL 10			
141 /			
142 X<>Y			
143 FS? 00		90	
144 GTO 00			
145 RTN			
146 *LBL 00			
147 /			
148 SQRT			
149 STO 02			
150 RTN			
151 *LBL 10			
152 ARCL X			
153 PROMPT			
154 "Re="			
	Output	00	



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**HP-41C**

**USERS' LIBRARY SOLUTIONS**

**Bar Codes**

**Solar Engineering**

## SOLAR ENGINEERING

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SOLAR BEAM  
IRRADIATION  
PROGRAM REGISTERS NEEDED: 89

HELETT PACKARD  
SOLUTION BOOK:  
SOLAR ENGINEERING

ROW 1 (1 : 3)



ROW 2 (4 : 6)



ROW 3 (6 : 13)



ROW 4 (14 : 22)



ROW 5 (22 : 30)



ROW 6 (30 : 41)



ROW 7 (42 : 46)



ROW 8 (46 : 57)



ROW 9 (57 : 62)



ROW 10 (63 : 64)



ROW 11 (65 : 70)



ROW 12 (71 : 76)



ROW 13 (76 : 85)



ROW 14 (86 : 88)



ROW 15 (88 : 95)



ROW 16 (95 : 102)



ROW 17 (103 : 109)



ROW 18 (110 : 119)



ROW 19 (119 : 127)



ROW 20 (128 : 138)



ROW 21 (139 : 141)



ROW 22 (142 : 149)



ROW 23 (150 : 157)



ROW 24 (158 : 166)



ROW 25 (167 : 175)



ROW 26 (176 : 183)



ROW 27 (184 : 191)



ROW 28 (192 : 201)



ROW 29 (202 : 210)



ROW 30 (211 : 221)



ROW 31 (222 : 231)



ROW 32 (231 : 238)



ROW 33 (238 : 244)



ROW 34 (244 : 253)



ROW 35 (253 : 262)



ROW 36 (263 : 272)



ROW 37 (272 : 282)



ROW 38 (283 : 293)



ROW 39 (293 : 302)



ROW 40 (303 : 311)



ROW 41 (312 : 320)



ROW 42 (321 : 329)



ROW 43 (330 : 340)



ROW 44 (341 : 349)



ROW 45 (349 : 353)



ROW 46 (354 : 359)



ROW 47 (359 : 367)



ROW 48 (367 : 370)



SUN ALTITUDE AZIMUTH  
SOLAR POND ABSORPTION  
PROGRAM REGISTERS NEEDED: 48

ROW 1 (1 - 2)



ROW 2 (3 - 6)



ROW 3 (6 - 12)



ROW 4 (13 - 21)



ROW 5 (22 - 29)



ROW 6 (30 - 42)



ROW 7 (43 - 50)



ROW 8 (50 - 58)



ROW 9 (59 - 66)



ROW 10 (67 - 72)



ROW 11 (73 - 78)



ROW 12 (79 - 84)



ROW 13 (85 - 92)



ROW 14 (92 - 98)



ROW 15 (99 - 106)



ROW 16 (107 - 112)



ROW 17 (113 - 124)











ROW 18 (125 - 136)





SUN ALTITUDE AZIMUTH  
SOLAR POND ABSORPTION

ROW 19 (137 - 146)	
ROW 20 (147 - 153)	
ROW 21 (154 - 160)	
ROW 22 (160 - 169)	
ROW 23 (170 - 182)	
ROW 24 (183 - 195)	
ROW 25 (196 - 202)	
ROW 26 (203 - 205)	

ENERGY EQUIVALENTS  
FUELS AND PRICES  
PROGRAM REGISTERS NEEDED: 40

ROW 1 (1 - 3)



ROW 2 (4 - 8)



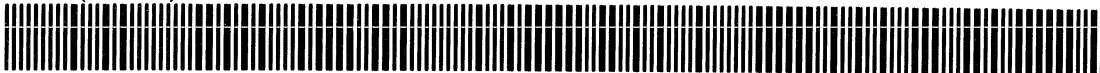
ROW 3 (8 - 14)



ROW 4 (15 - 19)



ROW 5 (20 - 27)



ROW 6 (27 - 28)



ROW 7 (28 - 34)



ROW 8 (34 - 41)



ROW 9 (41 - 48)



ROW 10 (48 - 55)



ROW 11 (55 - 63)



ROW 12 (63 - 71)



ROW 13 (71 - 79)



ROW 14 (80 - 85)



ROW 15 (85 - 88)



ROW 16 (88 - 91)



ROW 17 (91 - 94)



ROW 18 (95 - 98)



ENERGY EQUIVALENTS  
FUELS AND PRICES

ROW 19 (99 - 101)



ROW 20 (101 - 104)



ROW 21 (104 - 108)



ROW 22 (109 - 112)



HEAT EXCHANGERS

PROGRAM REGISTERS NEEDED: 67

ROW 1 (1 - 4)



ROW 2 (4 - 6)



ROW 3 (6 - 11)



ROW 4 (11 - 14)



ROW 5 (15 - 20)



ROW 6 (20 - 26)



ROW 7 (27 - 33)



ROW 8 (33 - 34)



ROW 9 (35 - 40)



ROW 10 (40 - 44)



ROW 11 (45 - 51)



ROW 12 (51 - 57)



ROW 13 (57 - 64)



ROW 14 (64 - 70)



ROW 15 (70 - 75)



ROW 16 (76 - 81)



ROW 17 (81 - 88)



ROW 18 (88 - 94)



# HEAT EXCHANGERS

ROW 19 (94 - 102)



ROW 20 (103 - 110)



ROW 21 (111 - 119)



ROW 22 (119 - 129)



ROW 23 (130 - 137)



ROW 24 (138 - 148)



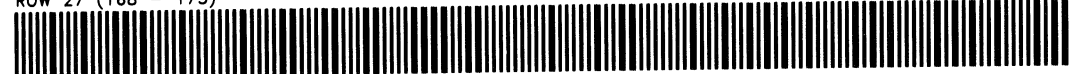
ROW 25 (149 - 161)



ROW 26 (162 - 168)



ROW 27 (168 - 175)



ROW 28 (176 - 183)



ROW 29 (184 - 196)



ROW 30 (197 - 203)



ROW 31 (204 - 206)



ROW 32 (206 - 210)



ROW 33 (211 - 216)



ROW 34 (217 - 224)



ROW 35 (225 - 230)



ROW 36 (231 - 234)



HEAT EXCHANGERS  
COUNTER FLOW  
PROGRAM REGISTERS NEEDED: 8

ROW 1 (1 - 6)



ROW 2 (7 - 19)



ROW 3 (19 - 25)



ROW 4 (26 - 36)



HEAT EXCHANGERS  
CROSS FLOW  
PROGRAM REGISTERS NEEDED: 14

ROW 1 (1 - 5)



ROW 2 (6 - 14)



ROW 3 (14 - 22)



ROW 4 (22 - 30)



ROW 5 (30 - 35)



ROW 6 (35 - 44)



ROW 7 (45 - 57)



ROW 8 (57 - 57)



HEAT EXCHANGERS  
PAR-COUNTER FLOW  
PROGRAM REGISTERS NEEDED: 12

ROW 1 (1 - 4)



ROW 2 (5 - 17)



ROW 3 (18 - 26)



ROW 4 (26 - 34)



ROW 5 (35 - 47)



ROW 6 (48 - 60)



ROW 7 (61 - 62)





HEAT EXCHANGERS  
PARALLEL FLOW  
PROGRAM REGISTERS NEEDED: 8

ROW 1 (1 - 6)



ROW 2 (7 - 19)



ROW 3 (19 - 25)



ROW 4 (26 - 36)



VIEW FACTOR

PROGRAM REGISTERS NEEDED: 23

ROW 1 (1 - 4)



ROW 2 (4 - 8)



ROW 3 (9 - 12)



ROW 4 (13 - 17)



ROW 5 (18 - 30)



ROW 6 (31 - 43)



ROW 7 (44 - 56)



ROW 8 (57 - 69)



ROW 9 (70 - 82)



ROW 10 (83 - 95)



ROW 11 (96 - 108)



ROW 12 (109 - 118)



ROW 13 (119 - 119)



HEAT TRANSFER THROUGH  
COMPOSITE CYLINDERS AND WALLS  
PROGRAM REGISTERS NEEDED: 26

ROW 1 (1 - 4)



ROW 2 (4 - 8)



ROW 3 (9 - 16)



ROW 4 (16 - 18)



ROW 5 (19 - 26)



ROW 6 (27 - 32)



ROW 7 (33 - 43)



ROW 8 (44 - 50)



ROW 9 (51 - 53)



ROW 10 (53 - 59)



ROW 11 (60 - 65)



ROW 12 (66 - 72)



ROW 13 (72 - 79)



RCW 14 (79 - 83)



BLACK BODY THERMAL RADIATION

PROGRAM REGISTERS NEEDED: 48

ROW 1 (1 - 4)



ROW 2 (4 - 10)



ROW 3 (10 - 13)



ROW 4 (13 - 17)



ROW 5 (17 - 20)



ROW 6 (20 - 23)



ROW 7 (23 - 27)



ROW 8 (27 - 30)



ROW 9 (30 - 33)



ROW 10 (33 - 36)



ROW 11 (36 - 42)



ROW 12 (42 - 49)



ROW 13 (49 - 57)



ROW 14 (58 - 62)



ROW 15 (63 - 75)



ROW 16 (76 - 83)



ROW 17 (83 - 95)



ROW 18 (96 - 108)



# BLACK BODY THERMAL RADIATION

ROW 19 (109 - 121)



ROW 20 (122 - 131)



ROW 21 (131 - 141)



ROW 22 (142 - 146)



ROW 23 (147 - 149)



ROW 24 (149 - 158)



ROW 25 (159 - 167)



ROW 26 (167 - 170)



ECONOMIC BREAK EVEN  
FOR SOLAR EQUIPMENT  
PROGRAM REGISTERS NEEDED: 21

ROW 1 (1 - 4)



ROW 2 (4 - 7)



ROW 3 (8 - 12)



ROW 4 (13 - 15)



ROW 5 (16 - 21)



ROW 6 (21 - 27)



ROW 7 (28 - 35)



ROW 8 (36 - 47)



ROW 9 (47 - 57)



ROW 10 (58 - 62)



ROW 11 (63 - 72)



# SOLAR PANEL ARRAY

PROGRAM REGISTERS NEEDED: 46

ROW 1 (1 - 3)



ROW 2 (4 - 5)



ROW 3 (6 - 14)



ROW 4 (15 - 24)



ROW 5 (25 - 35)



ROW 6 (36 - 44)



ROW 7 (44 - 49)



ROW 8 (50 - 56)



ROW 9 (57 - 65)



ROW 10 (66 - 75)



ROW 11 (76 - 83)



ROW 12 (83 - 88)



ROW 13 (89 - 94)



ROW 14 (95 - 100)



ROW 15 (100 - 102)



ROW 16 (103 - 111)



ROW 17 (111 - 121)



ROW 18 (122 - 126)



SOLAR PANEL ARRAY

ROW 19 (127 - 129)



ROW 20 (130 - 141)



ROW 21 (142 - 154)



ROW 22 (155 - 167)



ROW 23 (168 - 177)



ROW 24 (178 - 186)



ROW 25 (187 - 190)





CONDUIT FLOW

PROGRAM REGISTERS NEEDED: 39

ROW 1 (1 - 2)



ROW 2 (2 - 8)



ROW 3 (8 - 14)



ROW 4 (15 - 20)



ROW 5 (21 - 24)



ROW 6 (24 - 30)



ROW 7 (31 - 36)



ROW 8 (36 - 44)



ROW 9 (45 - 54)



ROW 10 (54 - 63)



ROW 11 (64 - 69)



ROW 12 (70 - 79)



ROW 13 (80 - 88)



ROW 14 (89 - 97)



ROW 15 (98 - 110)



ROW 16 (111 - 122)



ROW 17 (123 - 131)



ROW 18 (132 - 143)



CONDUIT FLOW

ROW 19 (144 - 154)



ROW 20 (154 - 161)



ROW 21 (161 - 165)



## NOTES

## NOTES

## NOTES

## NOTES

## NOTES

## NOTES



**NOTES**



Rev. B

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Statistics  
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Mechanical Engineering  
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Calendars  
Cardiac/Pulmonary  
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Physics  
Surveying**

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CONDUIT FLOW

